

# Special use of correctors for uncommon experiments: free electron orbital angular momentum and beyond

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With contributions from

Vienna: Thomas Schachinger, Stefan Löffler, and Peter Schattschneider

Modena: Vincenzo Grillo and his co-workers

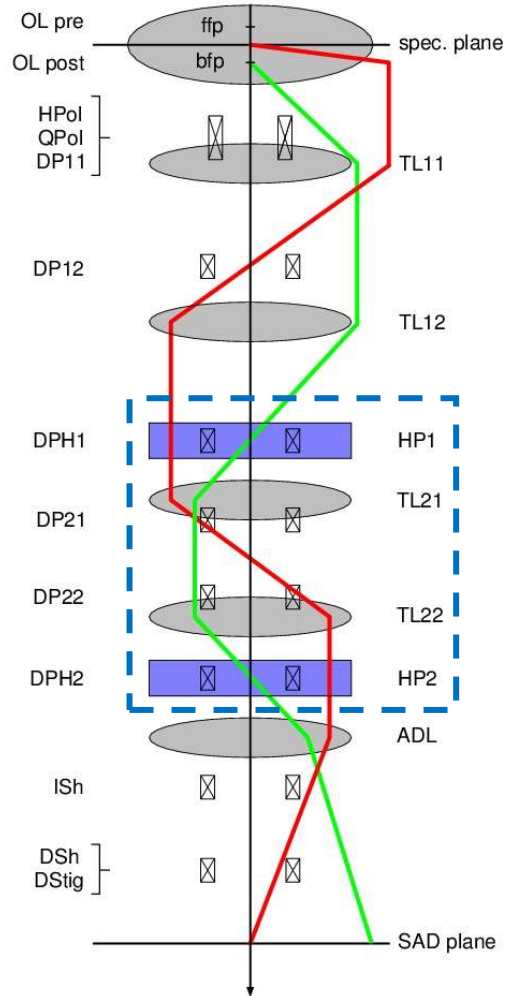
Heidelberg: Peter Hartel and Martin Linck

Berlin: Tolga Wagner

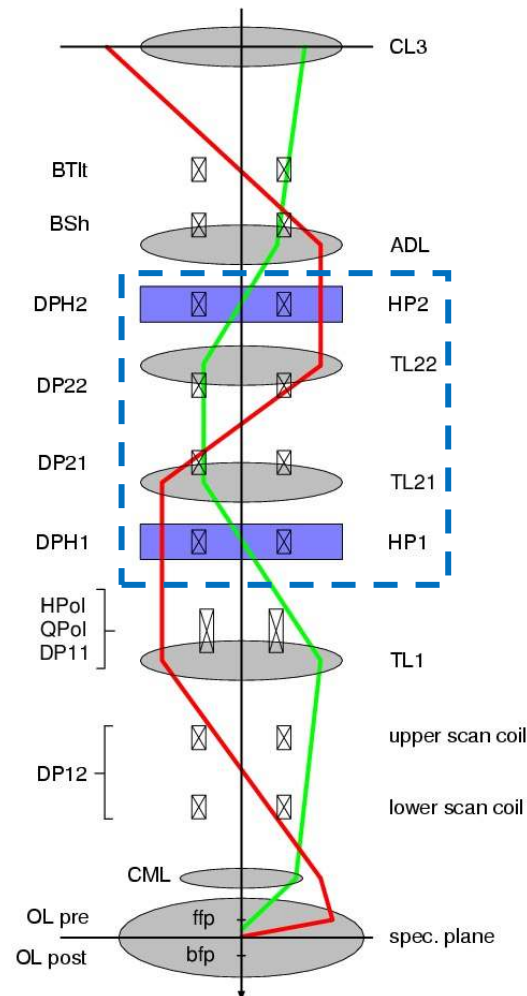
Juelich: Amir Tavabi and Rafal E. Dunin-Borkowski

# Cs corrector as an electron optical bench

CETCOR - CTEM

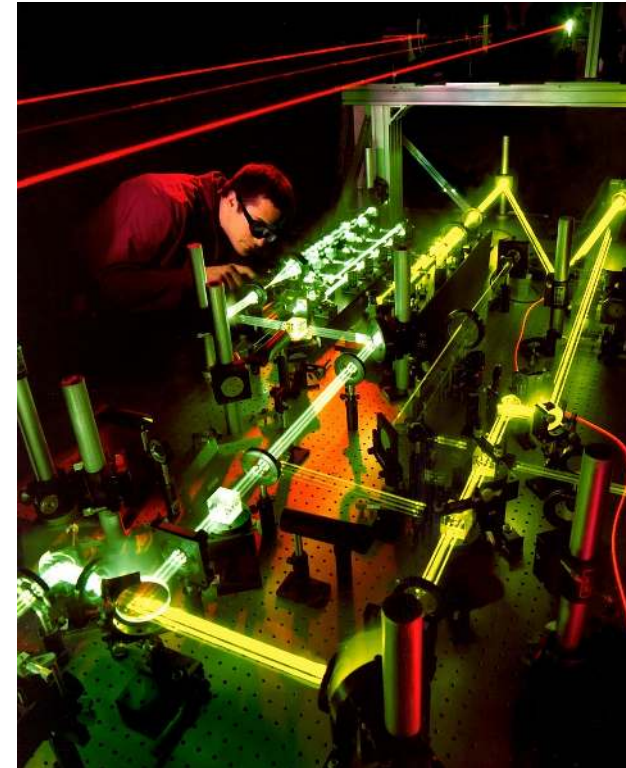


CESCOR - STEM



Not only **double hexapole** for aberration correction, but also **additional deflectors, dipoles, quadrupoles, hexapoles and transfer lenses** for alignment and correcting parasitic aberrations.

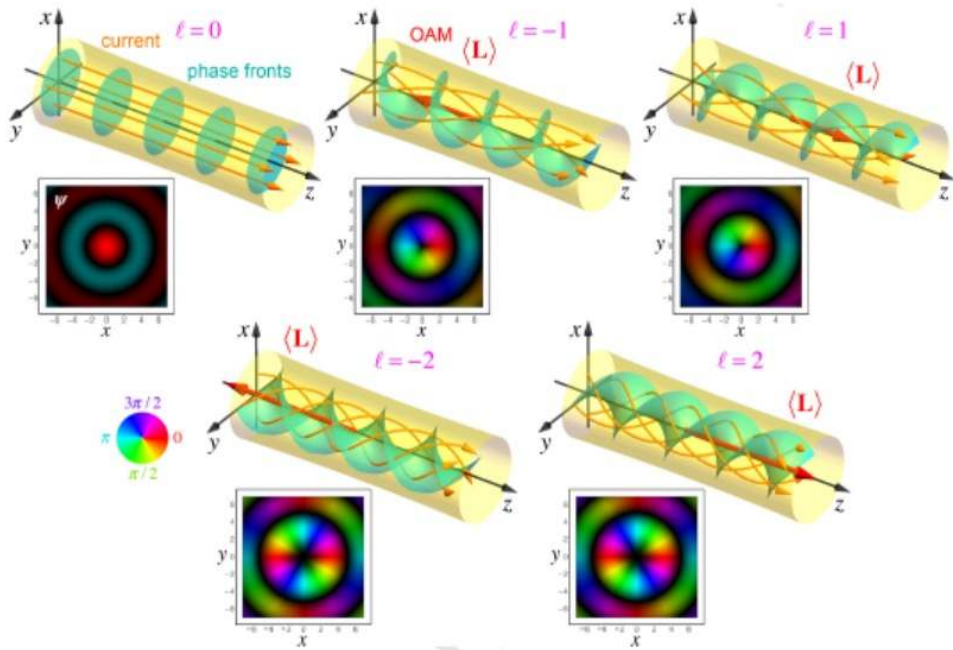
We could also treat it as an electron optical bench!



<https://www.ceos-gmbh.de/en/produkte/residualsCEXCOR>

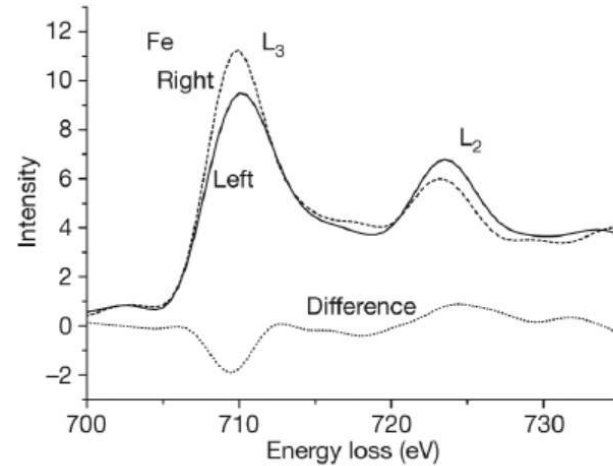
<https://www.needpix.com/photo/47763/>

# Orbital angular momentum of free electrons



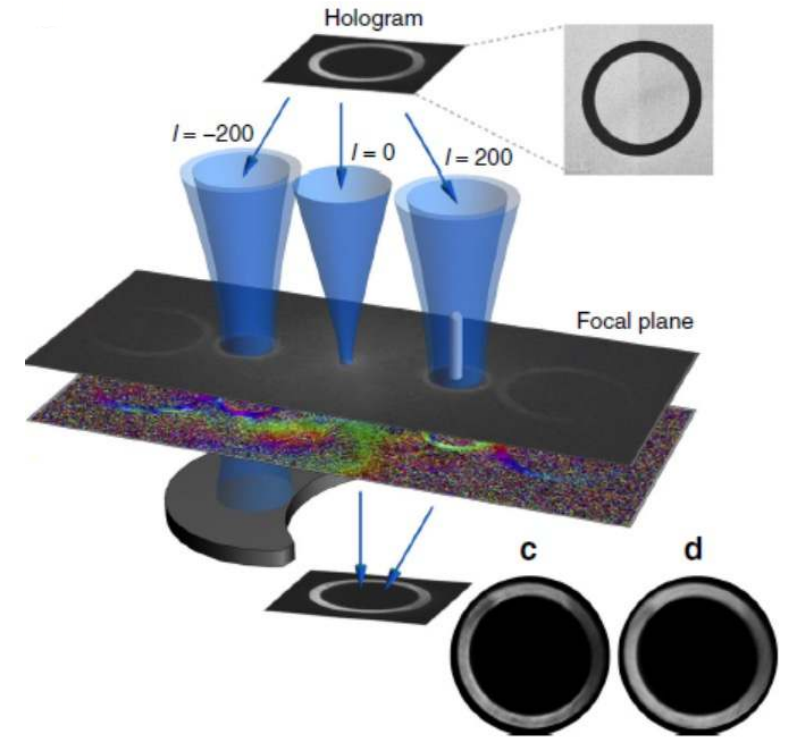
K.Y. Bliokh *et al.* Physics Reports 690, 1 (2017)

Helical phase front  
Phase singularity on the axis  
**Orbital angular momentum**  
**Magnetic moment**



J. Verbeeck *et al.* Nature 467, 301 (2010)

**Inelastic scattering**  
Electron magnetic circular dichroism  
break symmetry of the  $p^\pm$  state excitation  
 **$l = \pm 1$  (selection rule)**



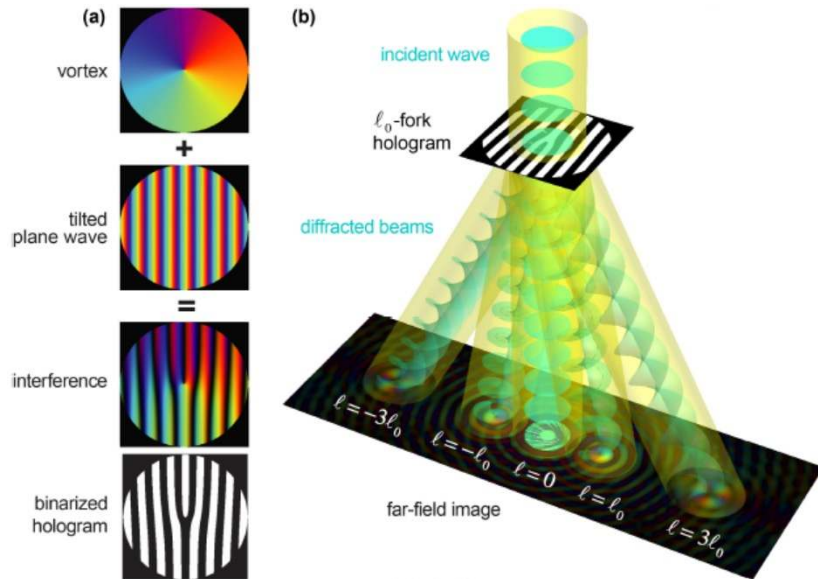
V. Grillo *et al.* Nat. Commun. 8, 689 (2017)  
A. Edström *et al.* PRL 116, 127203 (2016)

**Elastic scattering**  
Zeeman energy shift  
Intensity redistribution  
**larger OAM, better signal to noise ratio**



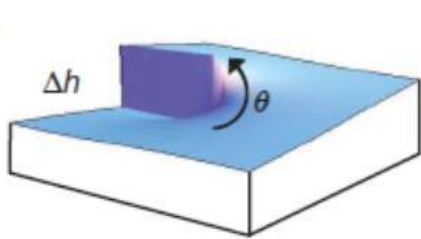
# How to produce free electron OAM?

## Diffractive hologram

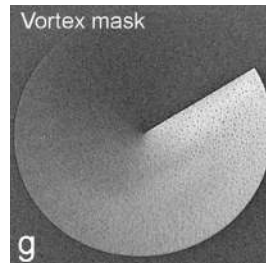


K.Y. Bliokh *et al.* Physics Reports 690, 1 (2017)

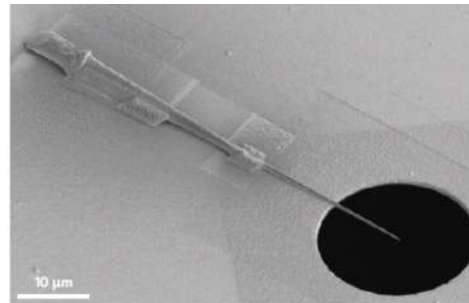
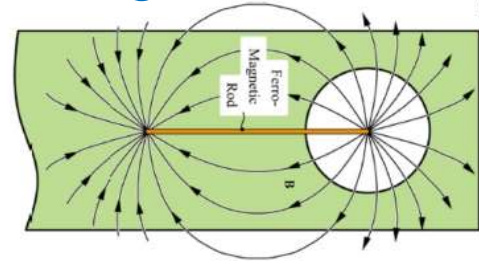
## Refractive phase plate



M. Uchida & A. Tonomura, Nature 464, 737 (2010) R. Shiloh *et al.* Ultramic. 144, 26 (2014)

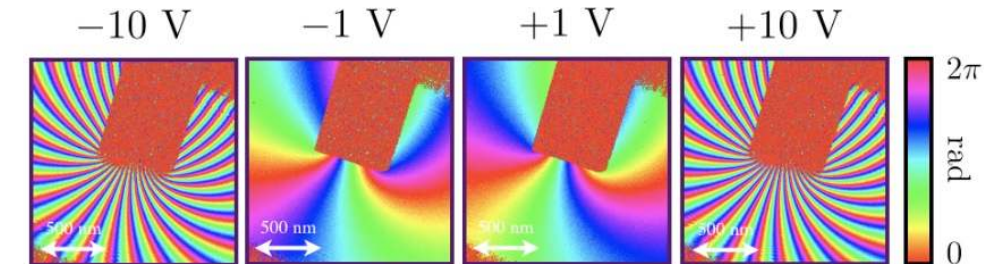
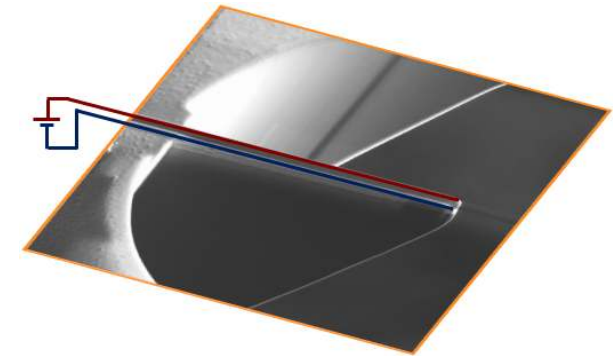
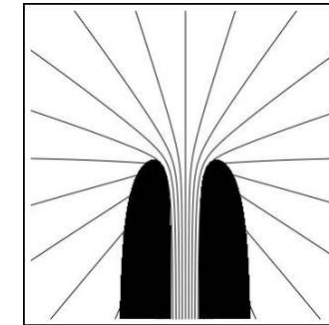


## Magnetic needle



A. Béché *et al.* Nat. Phys. 10, 26 (2014)  
A. M. Blackburn *et al.* Ultramic. 136, 127 (2014)

## Electrostatic chopstick



G. Pozzi *et al.* Ultramic. 181, 191 (2017)

A. Tavabi *et al.* Phys. Rev. Res. 2, 013185 (2020)

- Side lobes and transmission efficiency
- Device obstruction and possibly charging
- OAM mode purity
- Static or dynamic OAM modulation, etc.

## Alternative way: $\pi/2$ mode conversion

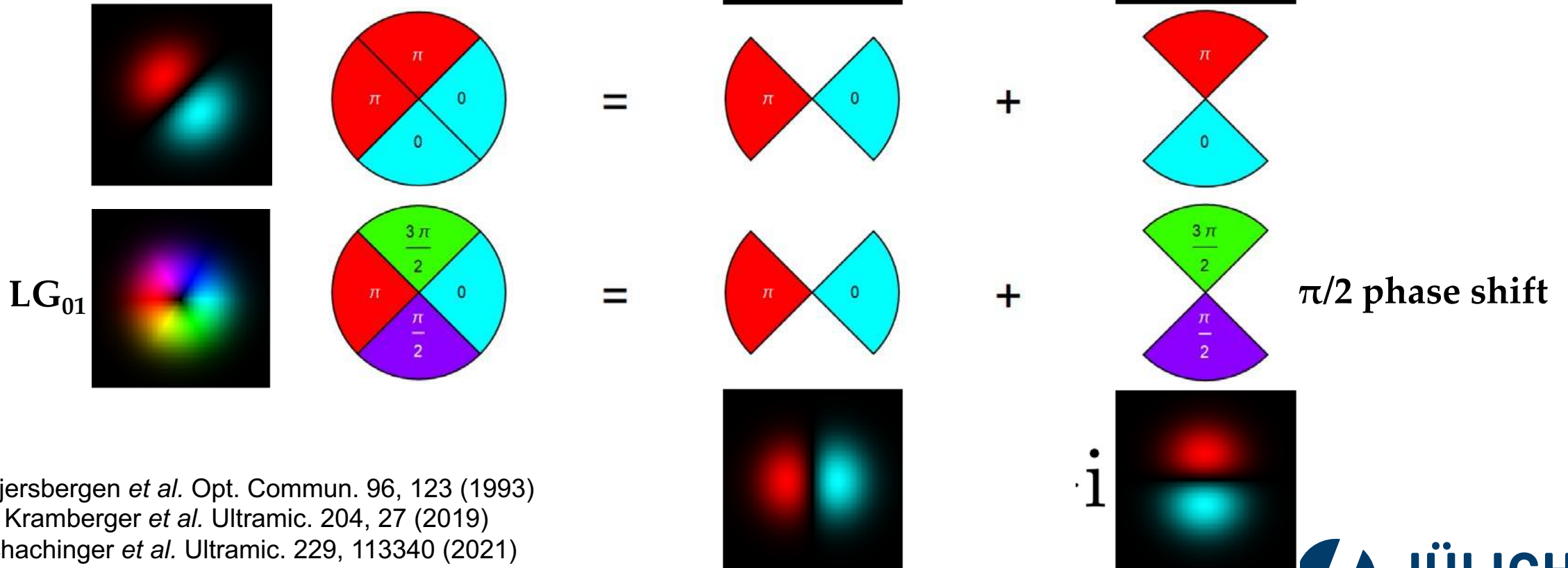
## Collaboration:

## TU Wien (Peter Schattschneider and his co-workers)

## CEOS (Peter Hartel)

FZ Juelich (Penghan Lu and Rafal Dunin-Borkowski)

## KIT (Dagmar Gerthen and her co-workers)



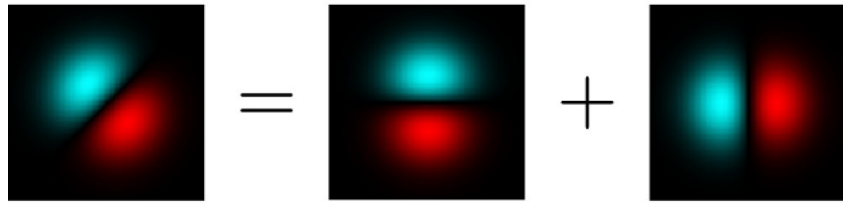
M. Beijersbergen *et al.* Opt. Commun. 96, 123 (1993)

C. Kramberger *et al.* Ultramic. 204, 27 (2019)

T. Schachinger *et al.* Ultramic. 229, 113340 (2021)

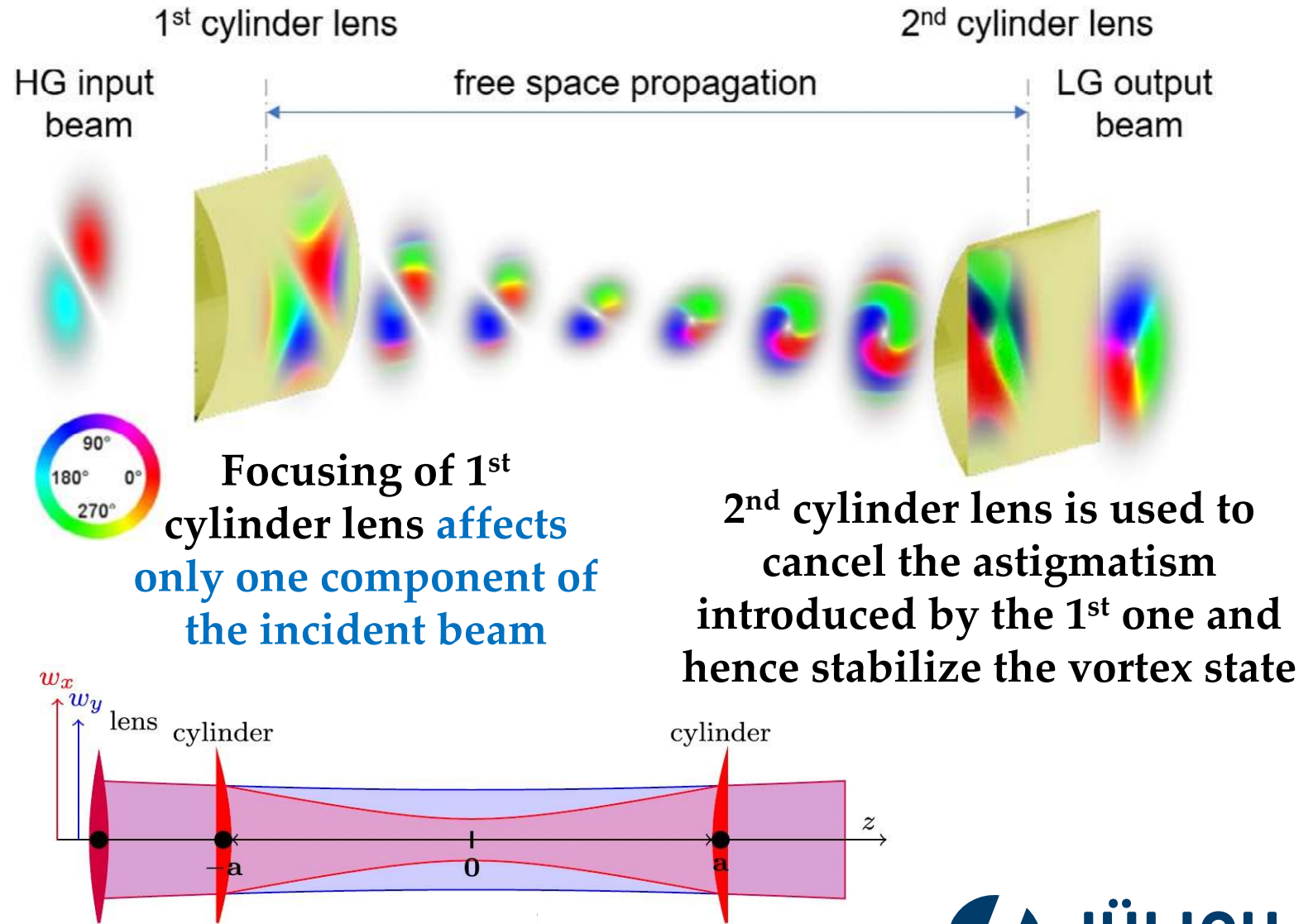
# How to achieve $\pi/2$ mode conversion?

HG beam at an angle of  $45^\circ$  with respect to cylinder lens orientation: superposition of 2 orthogonal HG modes



Focusing-induced Gouy phase retardation of  $\pi/2$

C. Kramberger *et al.* Ultramic. 204, 27 (2019)  
T. Schachinger *et al.* Ultramic. 229, 113340 (2021)



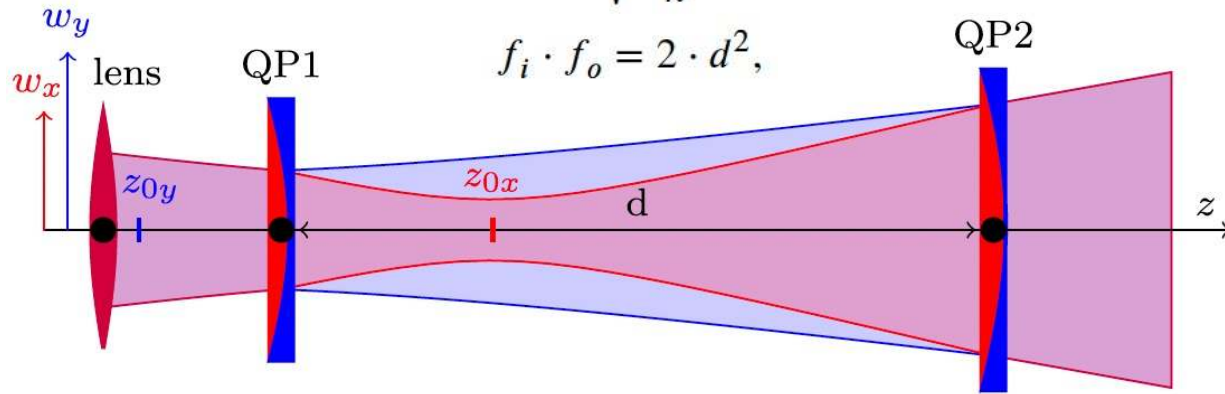


# But we don't have cylinder lens in the TEM...

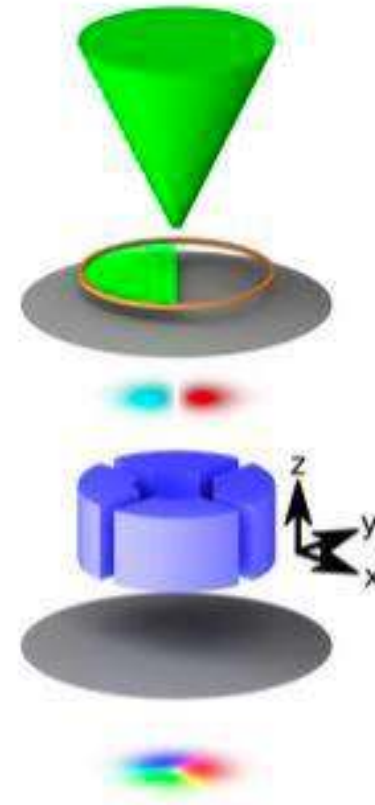
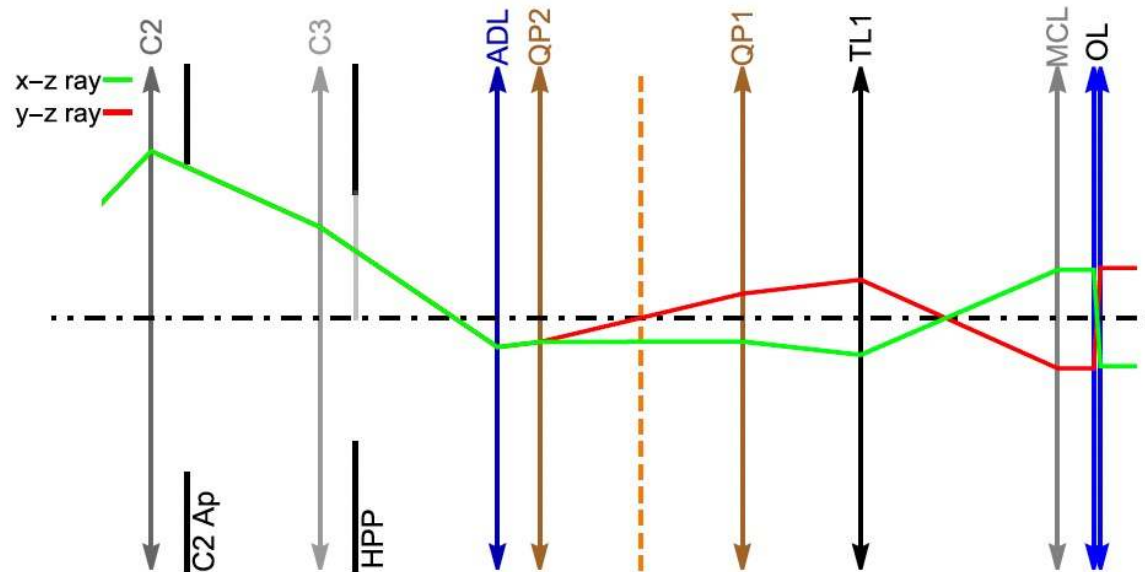
Asymmetric  
mode conversion

$$w_i = \sqrt{\frac{2f_i}{k}},$$

$$f_i \cdot f_o = 2 \cdot d^2,$$



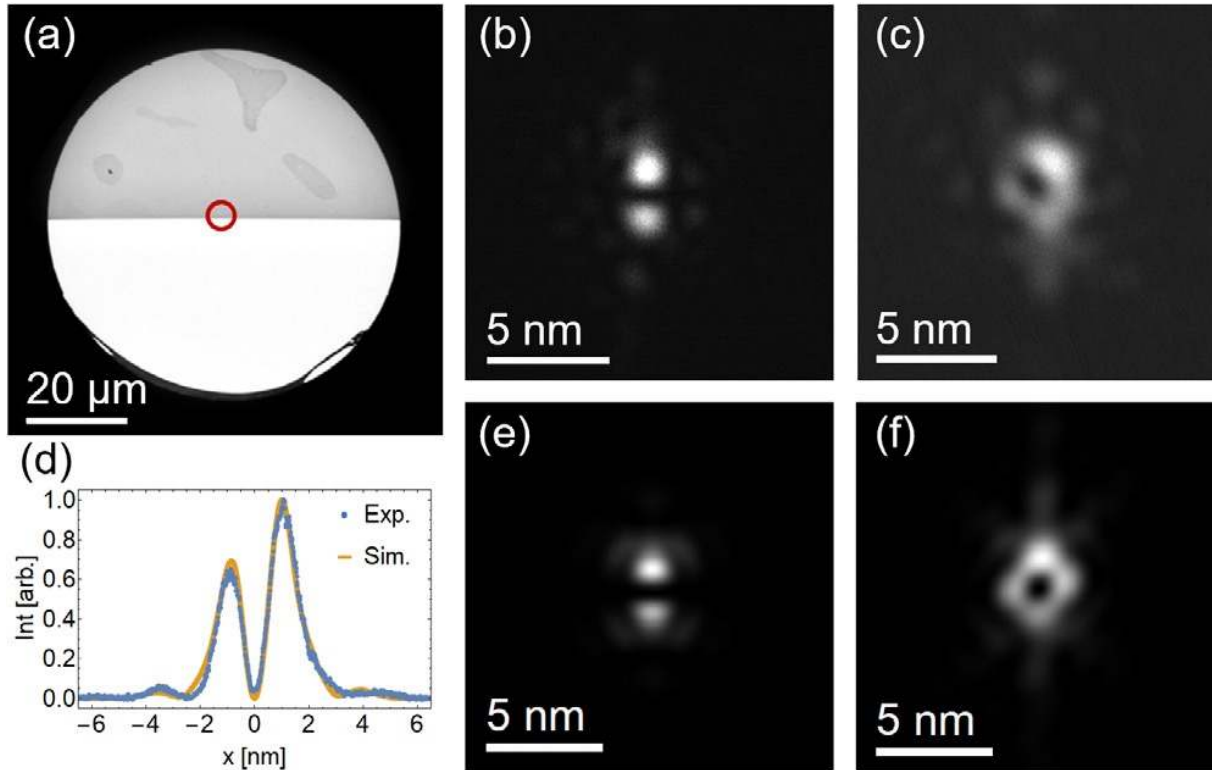
Instead we used **2 quadrupoles in the CEOS DCOR probe corrector** on Juelich Titan PICO microscope



C. Kramberger *et al.* Ultramic. 204, 27 (2019)  
T. Schachinger *et al.* Ultramic. 229, 113340 (2021)

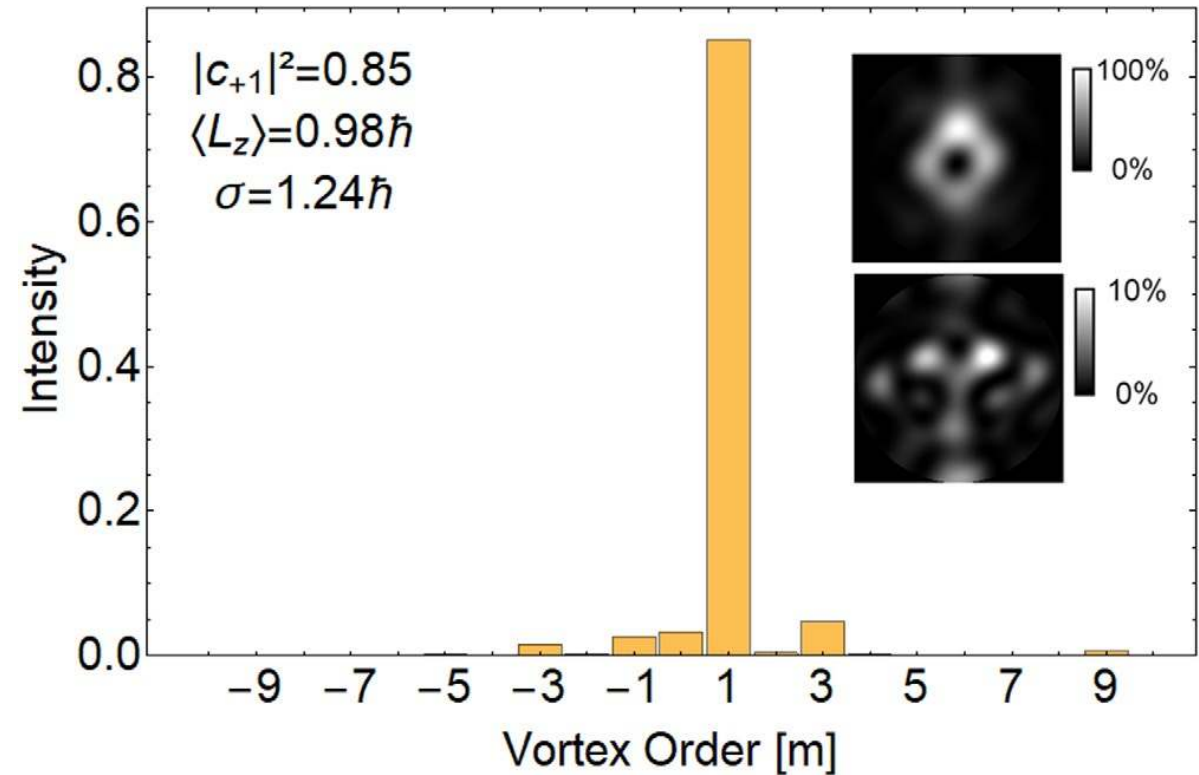
# Experimental demonstration

Experimental



Simulation

OAM spectrum decomposition by comparing with image simulation



T. Schachinger *et al.* Ultramic. 229, 113340 (2021)

Can we measure free electron OAM modes directly as a spectrum like e.g. EELS?

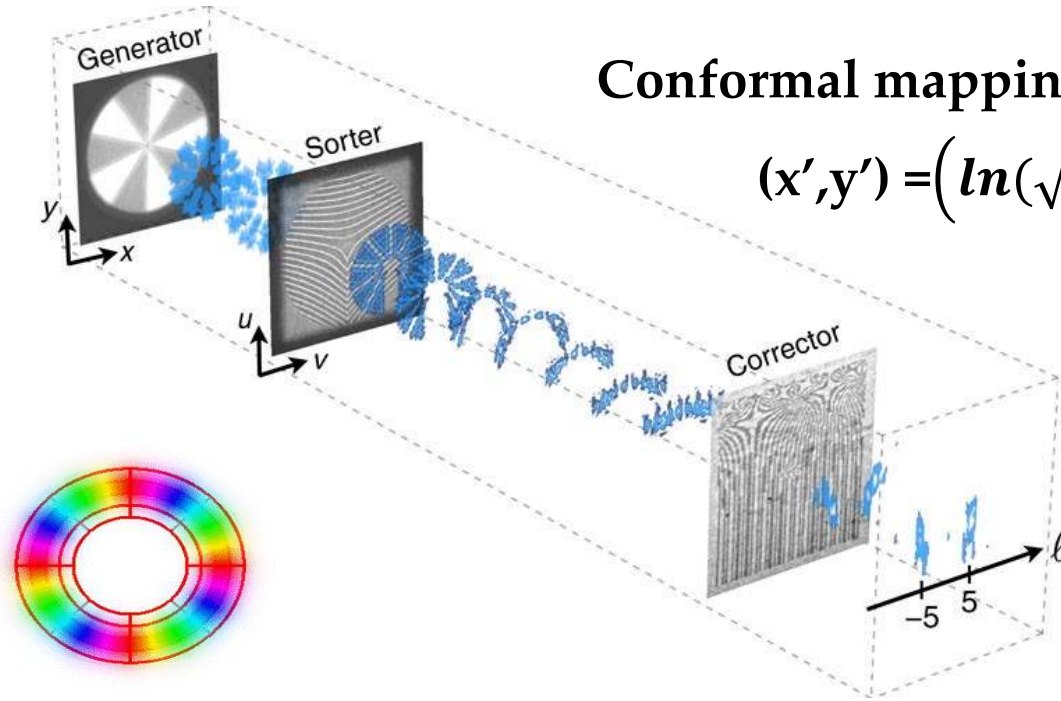


# OAM sorter

Collaboration:  
CNR (Vincenzo Grillo and his co-workers)  
FZ Juelich (Amir Tavabi and others)  
TFS (Peter Tiemeijer)

Conformal mapping: Log-polar transformation

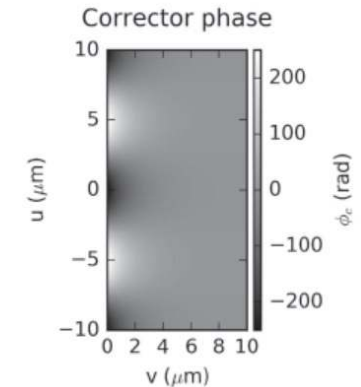
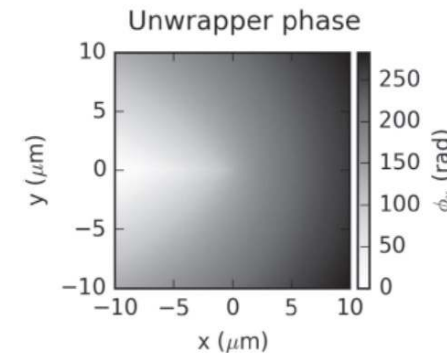
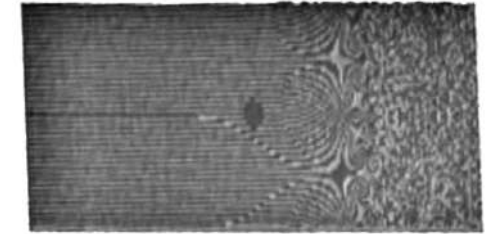
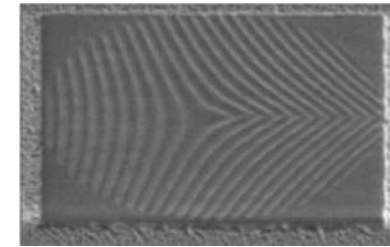
$$(x', y') = (\ln(\sqrt{x^2 + y^2}), \text{atan}(y/x))$$



The transformation of coordinates (in geometric optics approximation) transforms a vortex into a plane wave that can be analysed by a diffraction lens

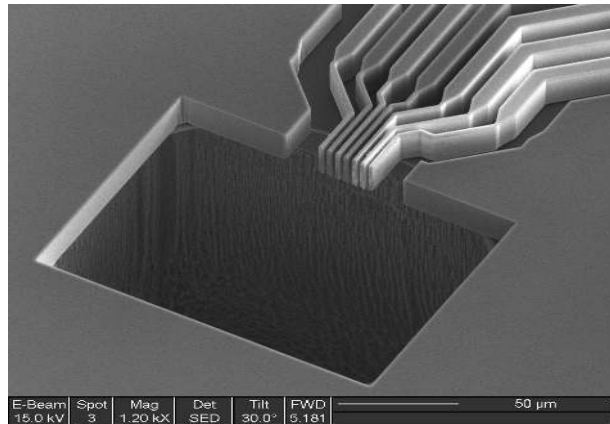
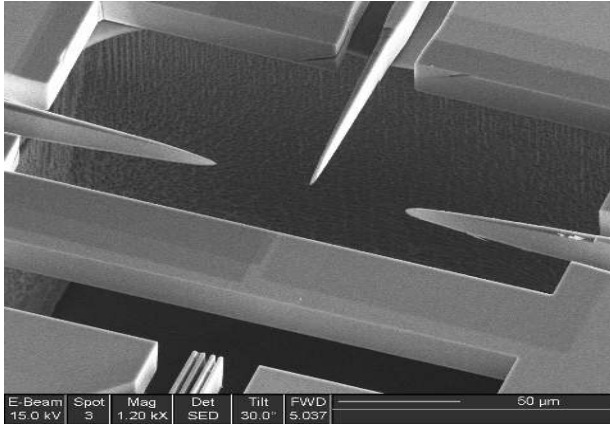
G.C.G. Berkhout *et al.* Phys. Rev. Lett. 105, 153601 (2010)  
V. Grillo *et al.* Nature Commun. 8, 15536 (2017)

Thin film-based holographic masks

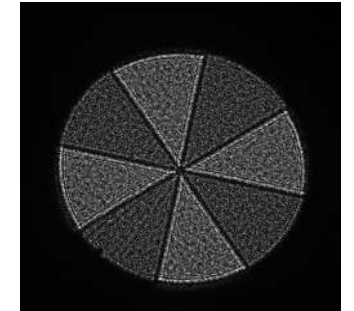
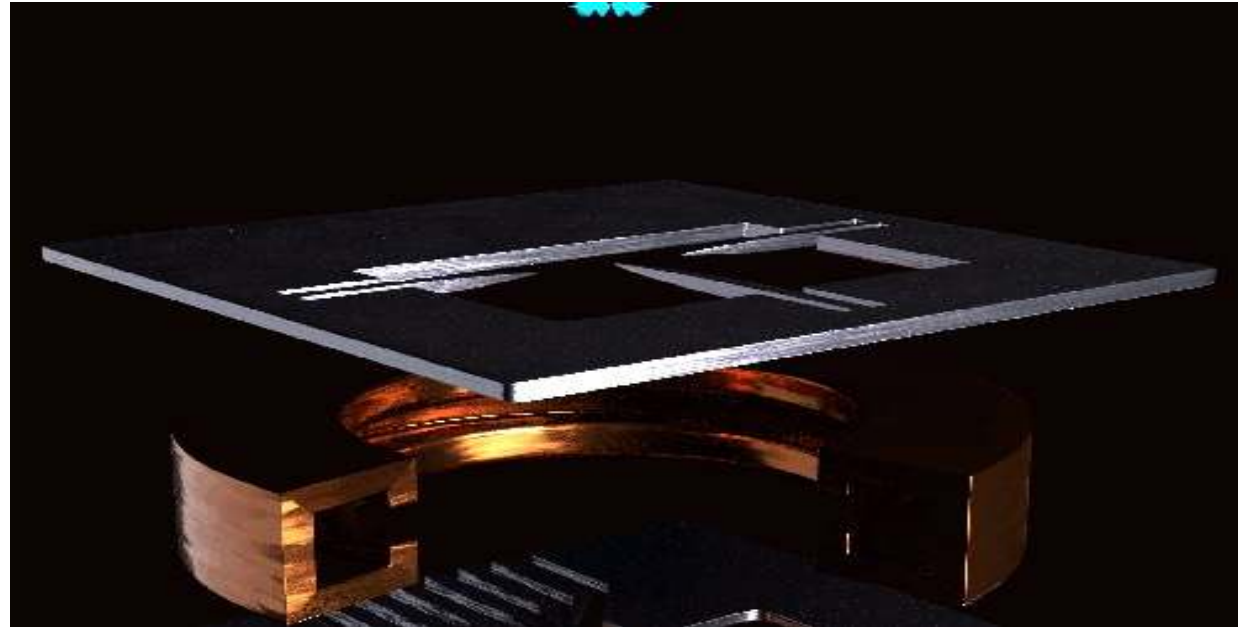


# Electrostatic OAM sorter

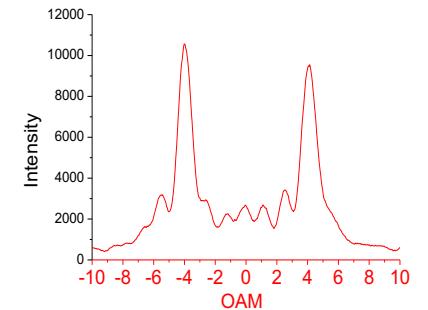
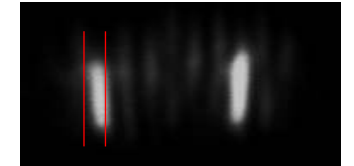
## Sorter-1 - OBJ aperture



## Sorter-2 - SAD aperture



$$\Delta L = 1.1 \hbar$$



A. Tavabi *et al.* Phys. Rev. Lett 126, 094802 (2021)

# Align sorter devices

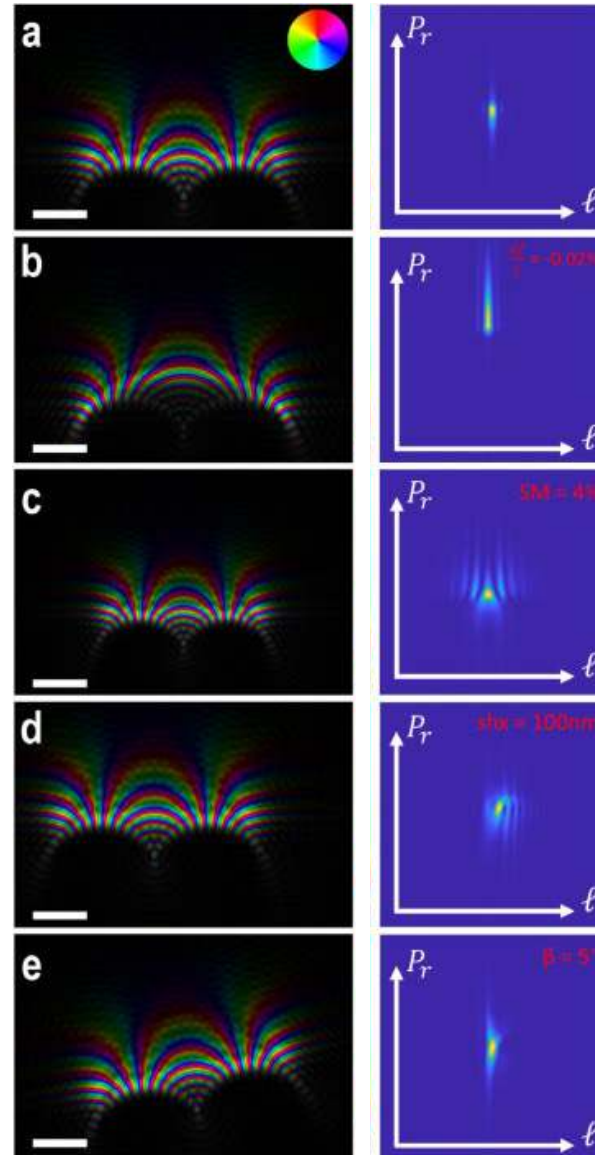
Ideal

Out of focus

Size mismatch

Lateral shift

Rotation



Match between S1 (OBJ) and S2 (SAD)  
– image corrector and XL lenses

Image corrector + XL  
lens combination  
to change focus

Image corrector + XL  
lens combination  
to change size

Deflectors

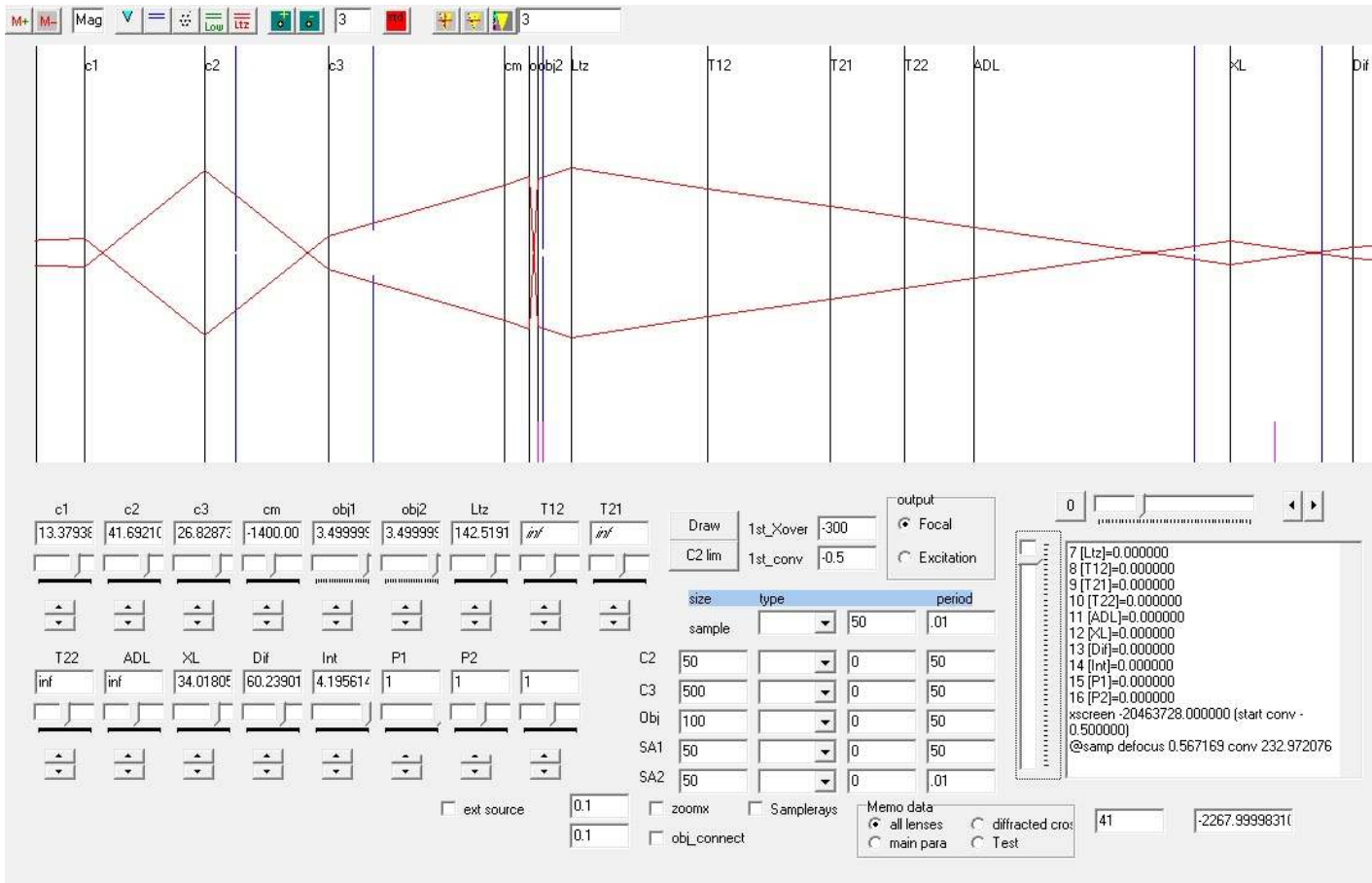
Image corrector + XL  
lens combination  
to change rotation



# Magnifying S1 image to S2

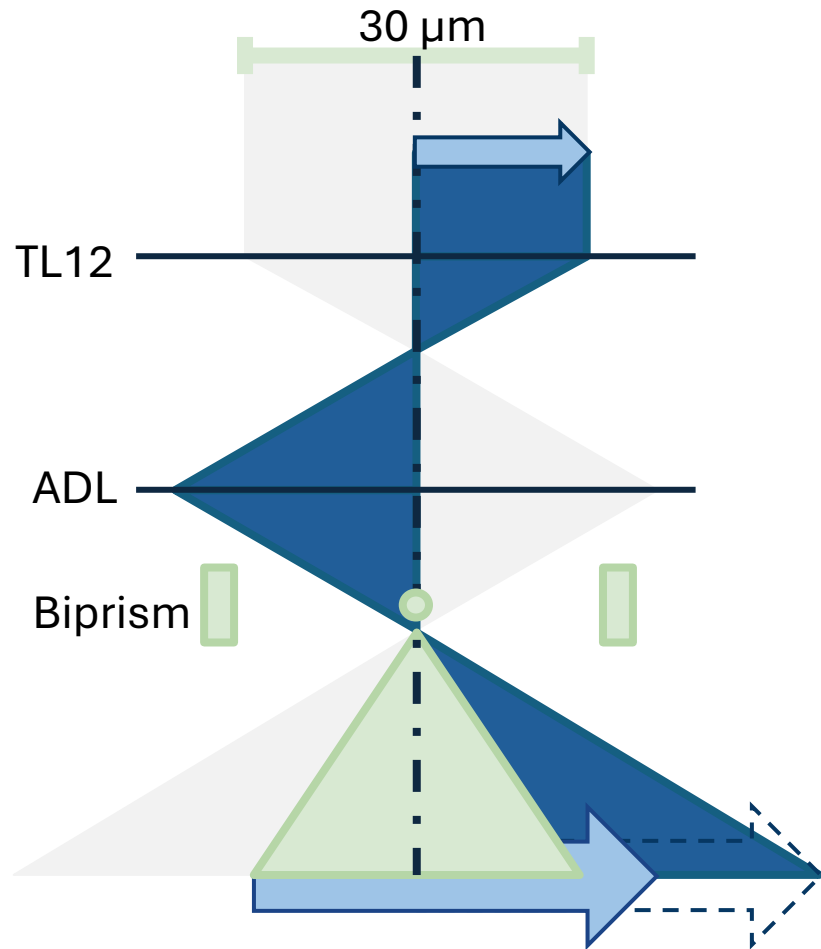
S1 (OBJ)

S2 (SAD)



- Nanofabrication limit to make S2 small
- Tuning the electrostatic field of S1 can help but a large excitation is undesirable because of parasitic large aberration
- Image corrector off (except TL11 and sometimes ADL) and excitation of XL produces an effective long camera length of  $f = 1.4$  m

# Similar tweaking corrector lens for large FoV holography



Credit: Tolga Wagner (HU Berlin) and Martin Linck (CEOS)

The large field of view holography was achieved by tuning final transfer lenses (TL12, ADL) of image corrector as a demagnifying objective and placing the crossover closer to the biprism plane, thus allowing a wide width of the interference pattern at medium interference fringe spacings.

**Alternative setup (developed by myself)**  
in OL-off LM mode reaching  $(10\text{-}40\text{ }\mu\text{m})^2$  interference FoV.

As an example, a  $22\mu\text{m} \times 22\mu\text{m}$  FoV holography reconstructed phase image from a phase plate device.

