

How do aberration correctors work?

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CEOS

Corrected Electron Optical
Systems GmbH



Invention of the Transmission Electron Microscope

CEOS

Corrected Electron Optical
Systems GmbH



1931, TU Berlin

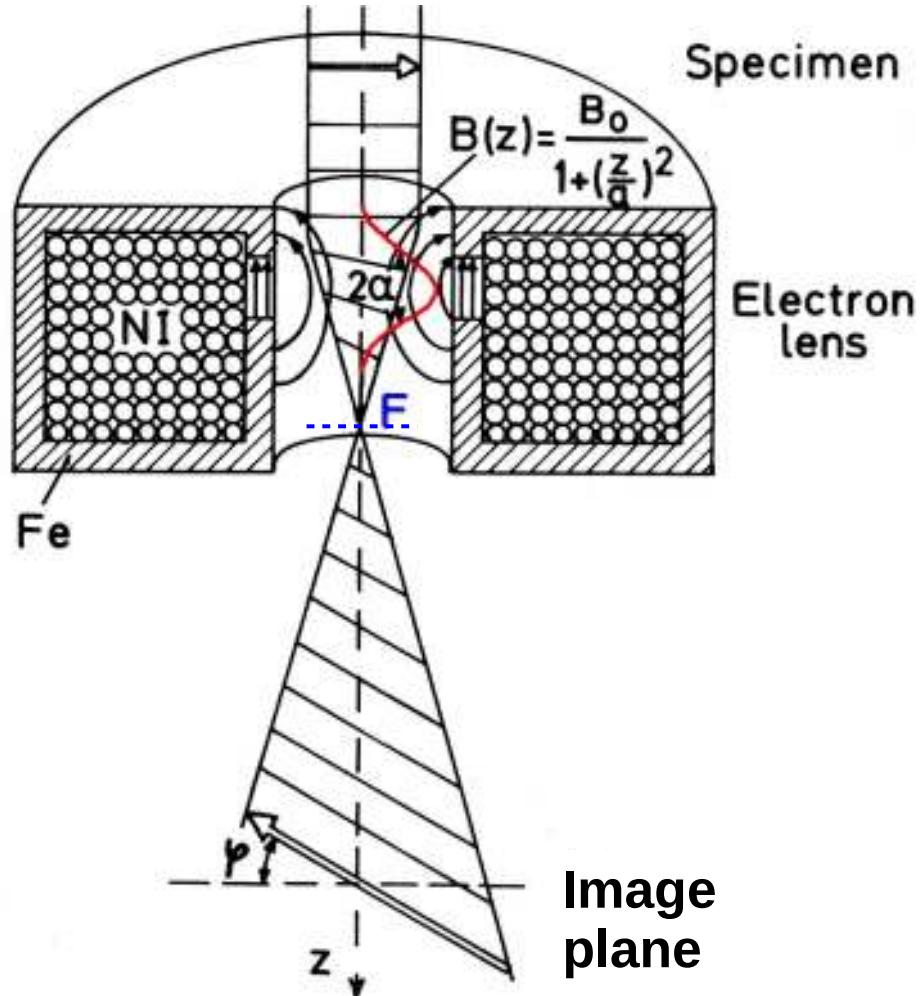
Ernst Ruska

Max Knoll



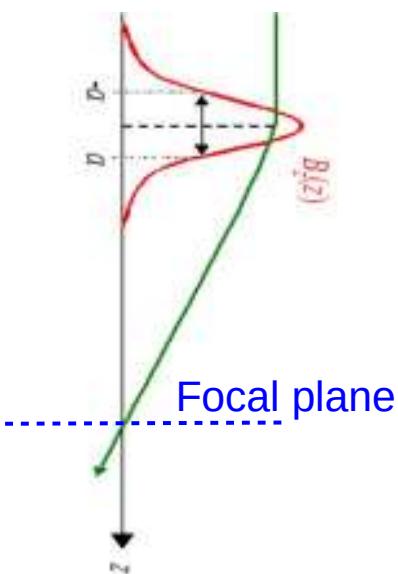


Magnetic Lens for Electrons



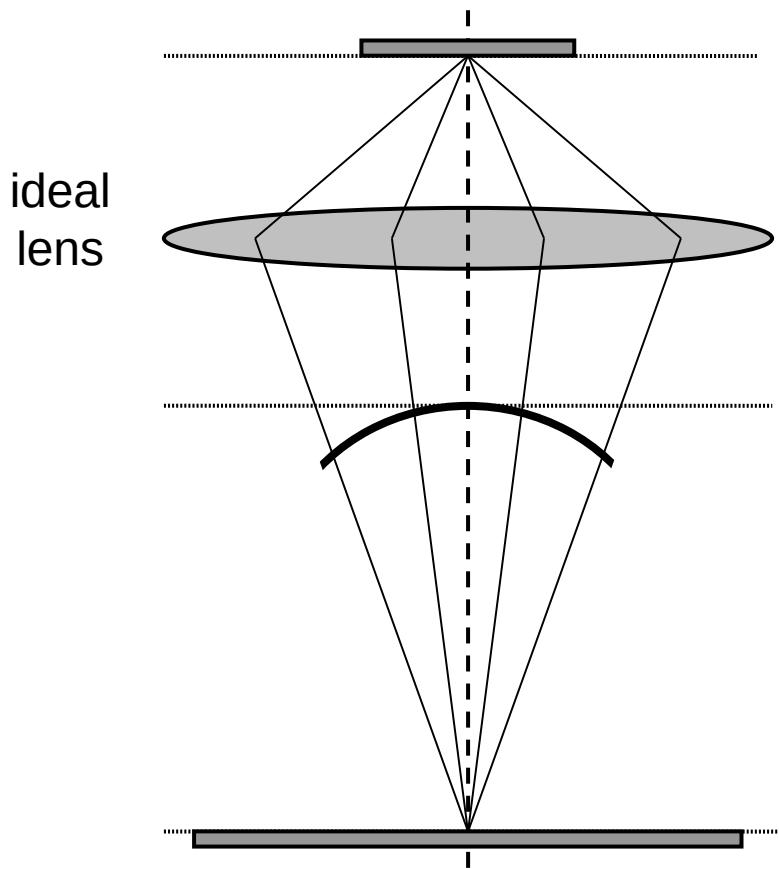
Glaser's "Glockenfeld"

bell-shaped,
axial magnetic field



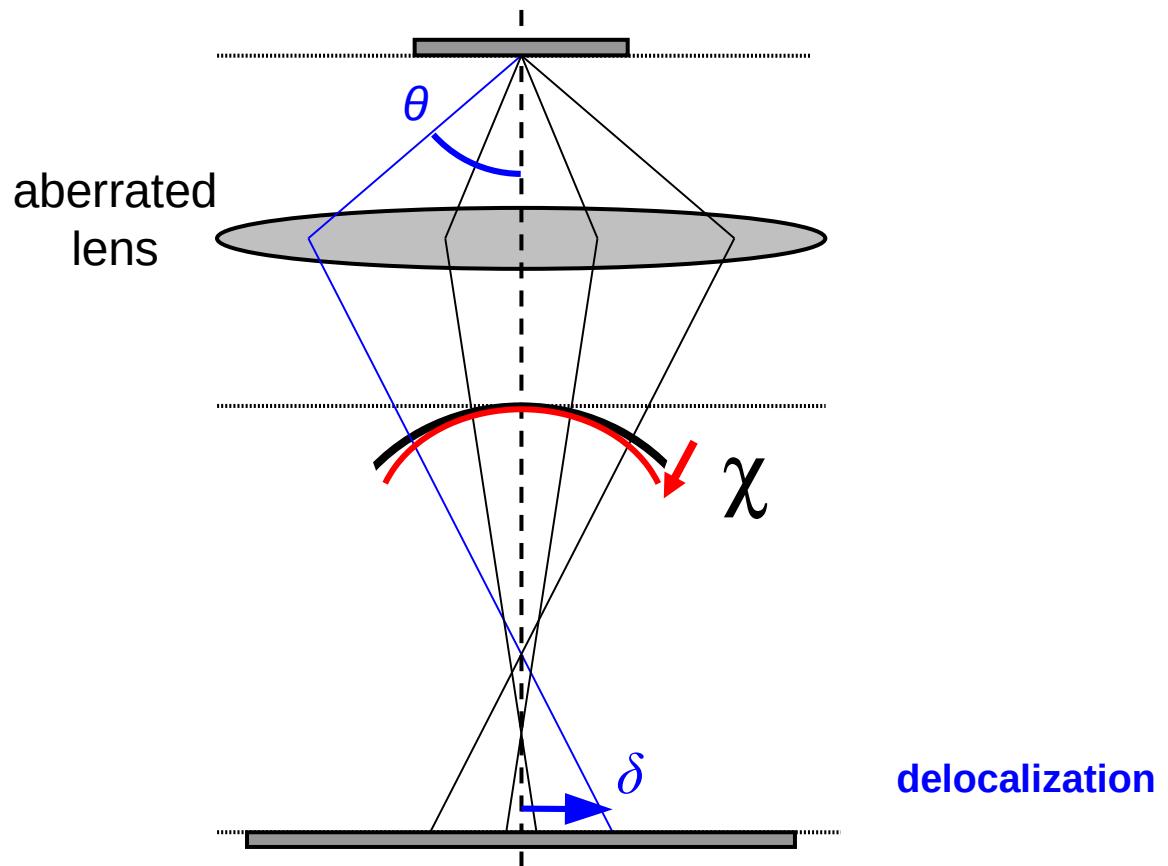


Lens aberrations



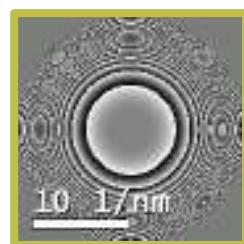
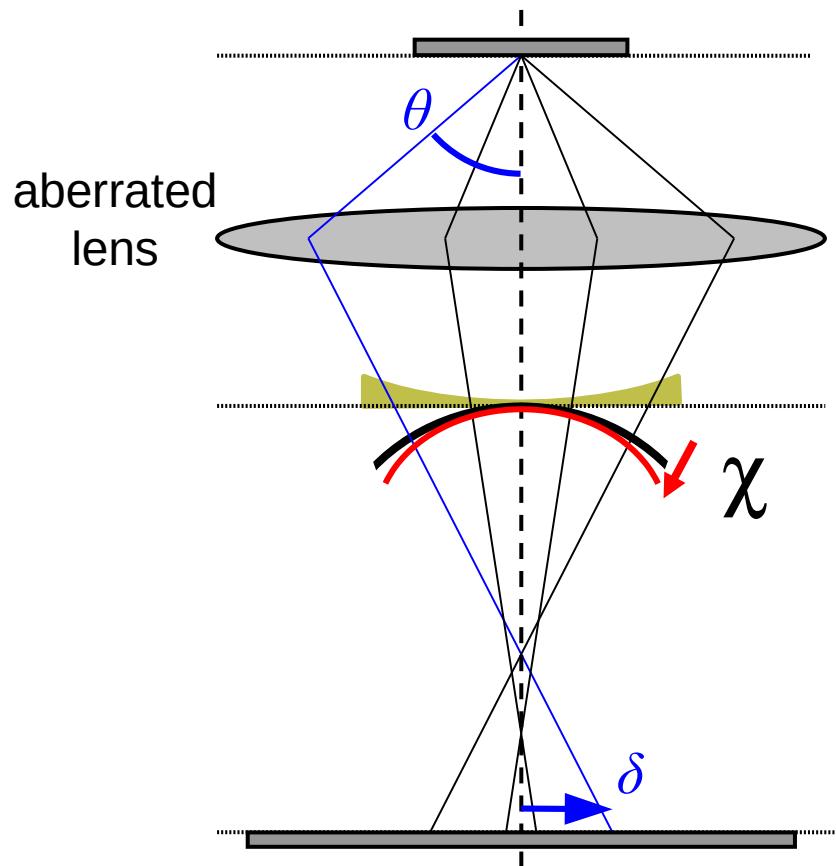


Lens aberrations: Spherical aberration



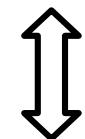


Lens aberrations: Spherical aberration



phase plate

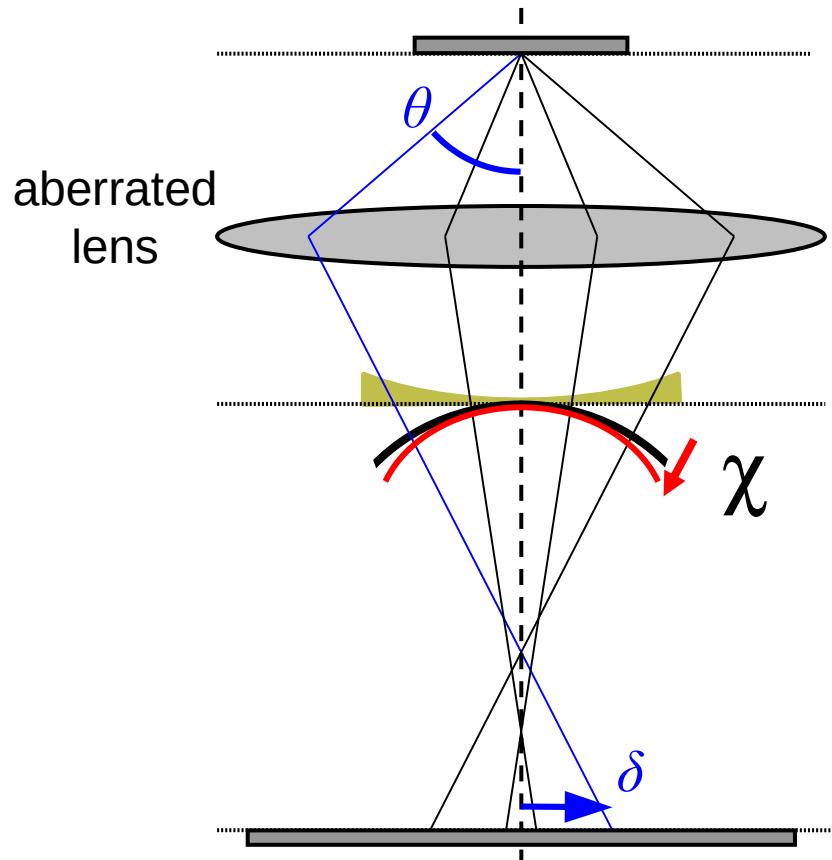
$$\exp\{-i\chi\} \quad \text{with} \quad \chi = \frac{2\pi}{\lambda} \cdot \frac{C_3}{4} \theta^4$$



$$\text{delocalization: } \delta = \frac{\nabla \chi}{2\pi} = C_3 \cdot \theta^3$$



Spherical aberration : Scherzer's Theorem



Über einige Fehler von Elektronenlinsen.

Von O. Scherzer in Darmstadt.

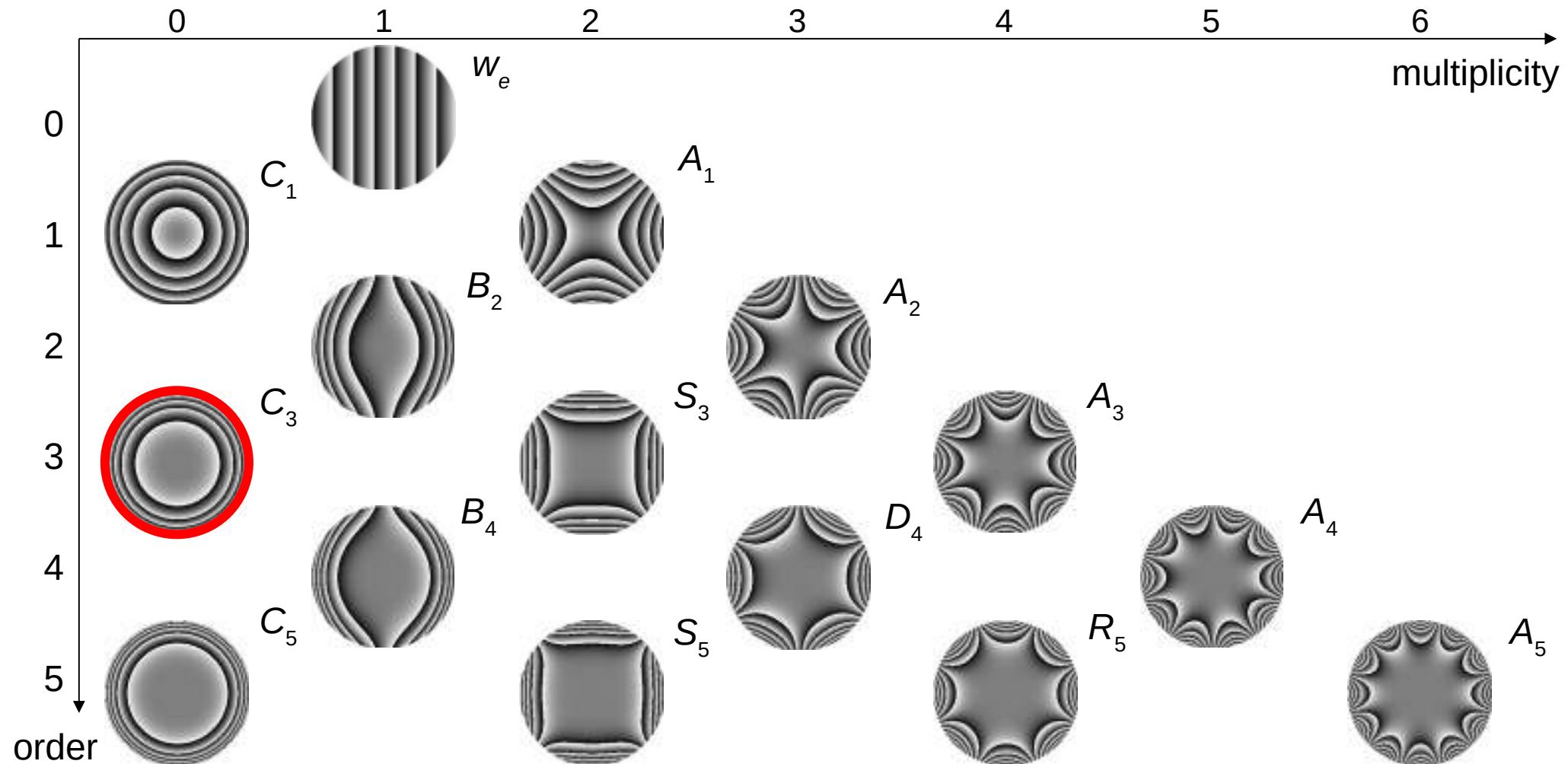
Mit 3 Abbildungen. (Eingegangen am 4. Juni 1936.)

Unmöglichkeit des Achromaten. Die Bildfehler dritter Ordnung. Unvermeidbarkeit der sphärischen Aberration.



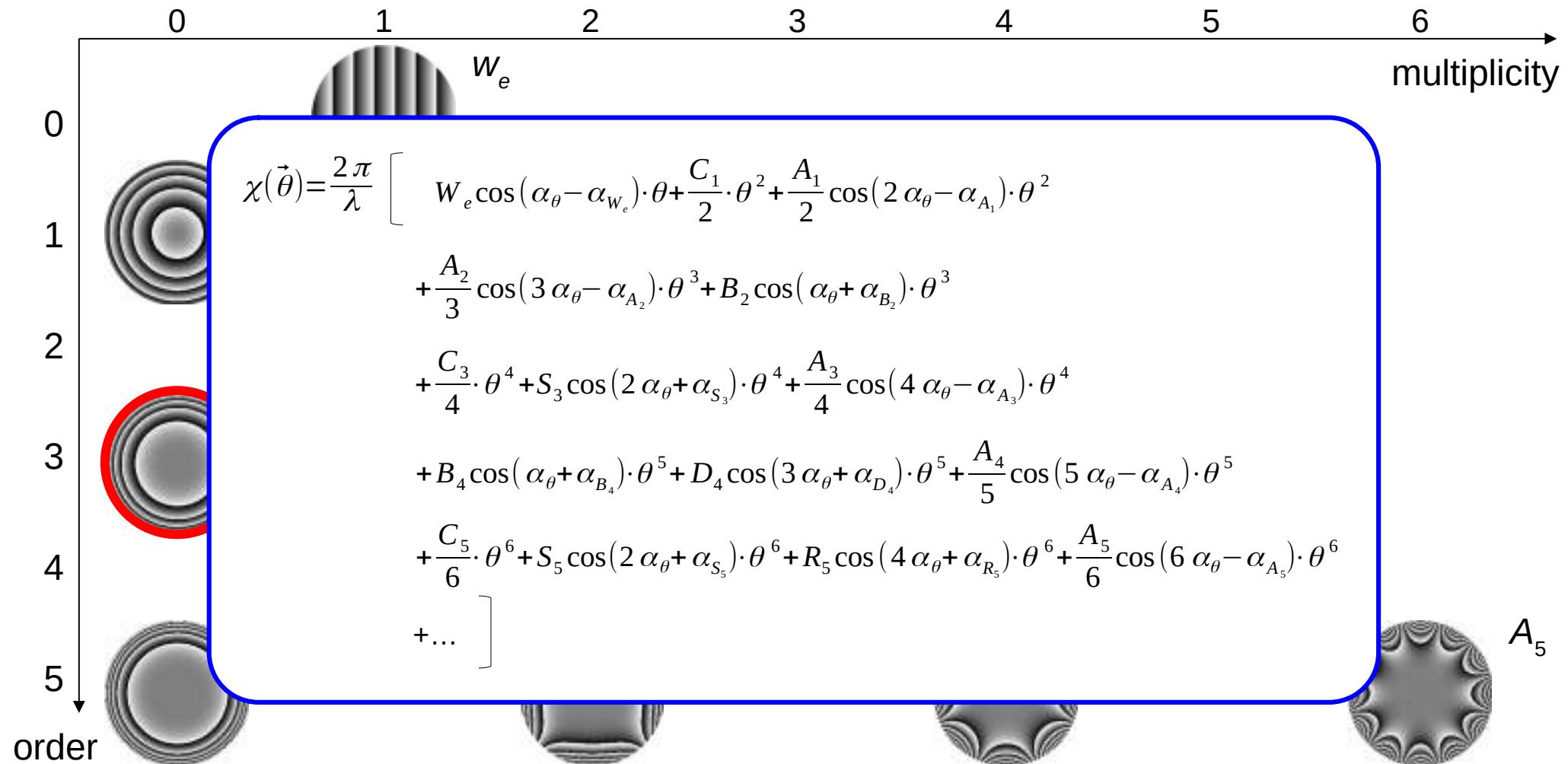
Unavoidable positive spherical aberration for stationary, space-charge-free, round electron lenses!

Prof. Otto Scherzer
(TU Darmstadt)

Wave aberration χ 

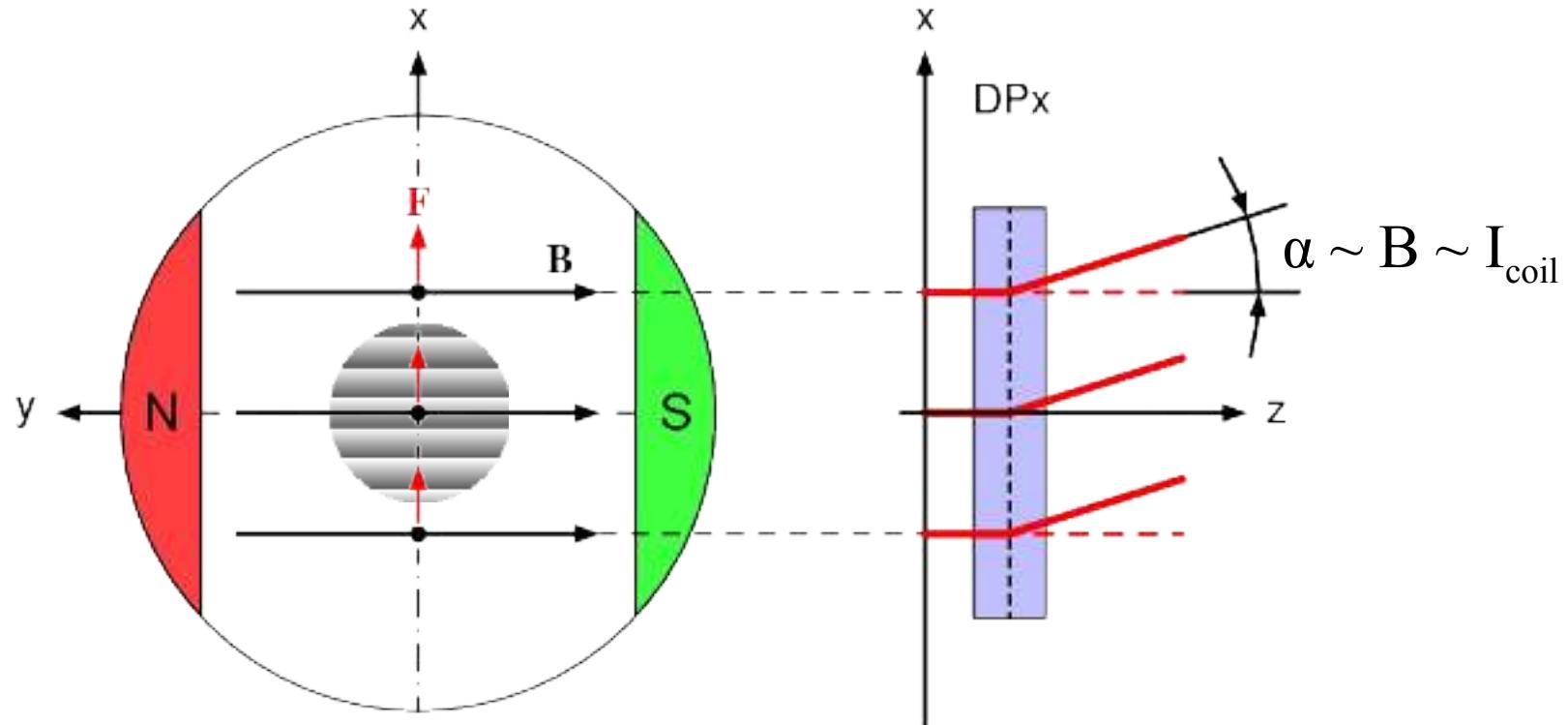


Wave aberration χ



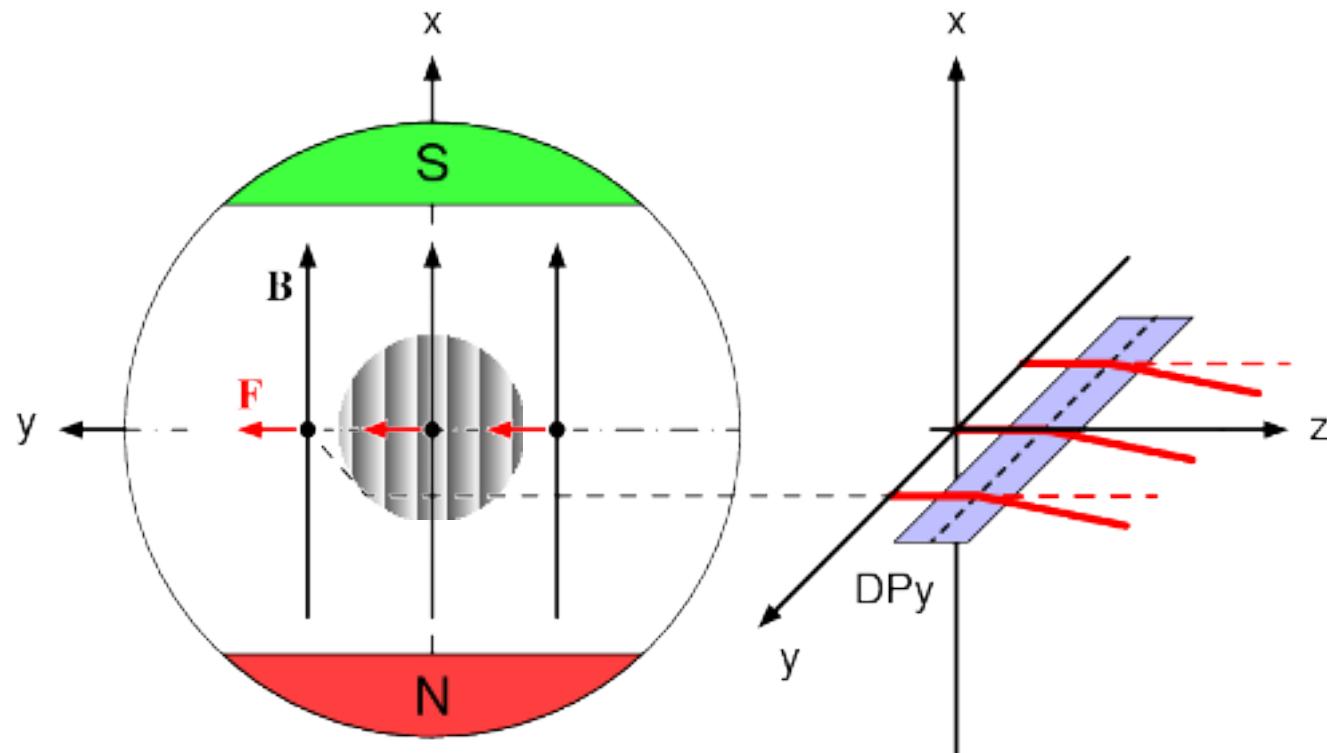


Dipoles – beam deflection in x-section



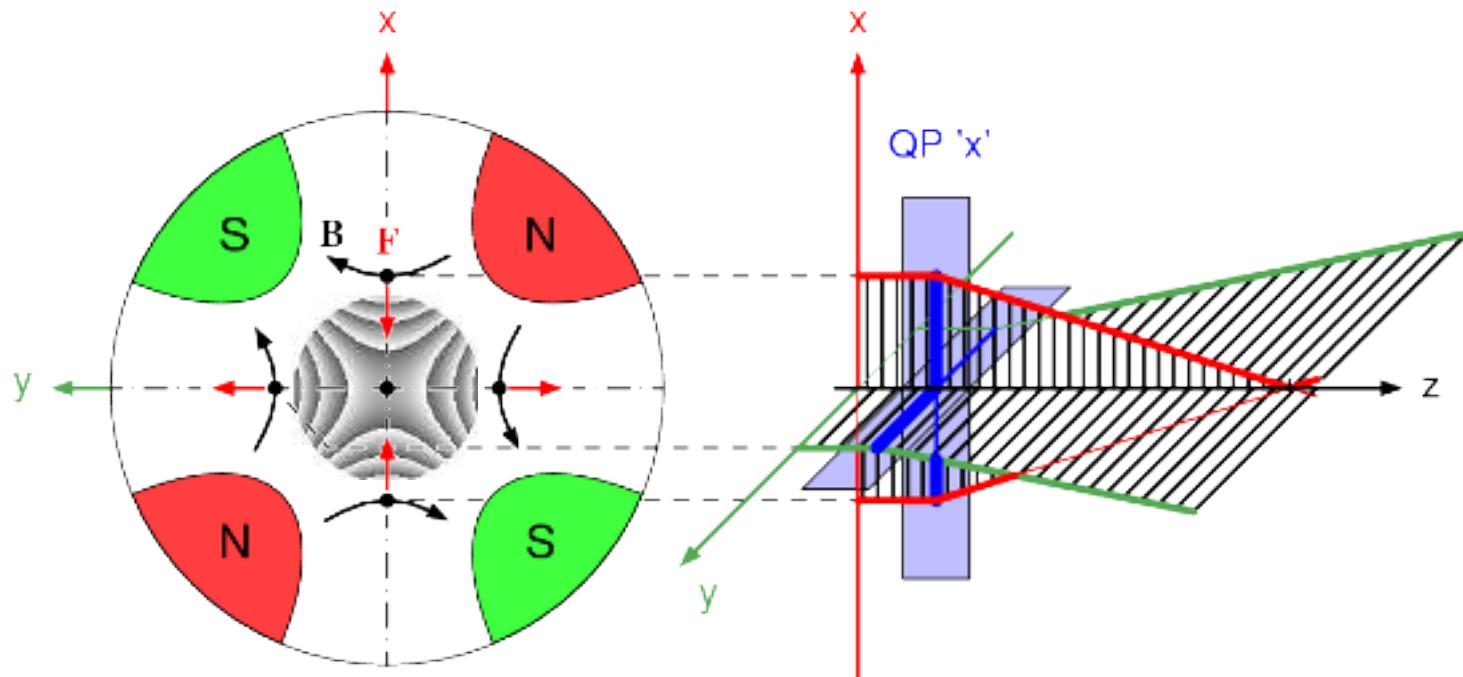


Dipoles – beam deflection in y-section



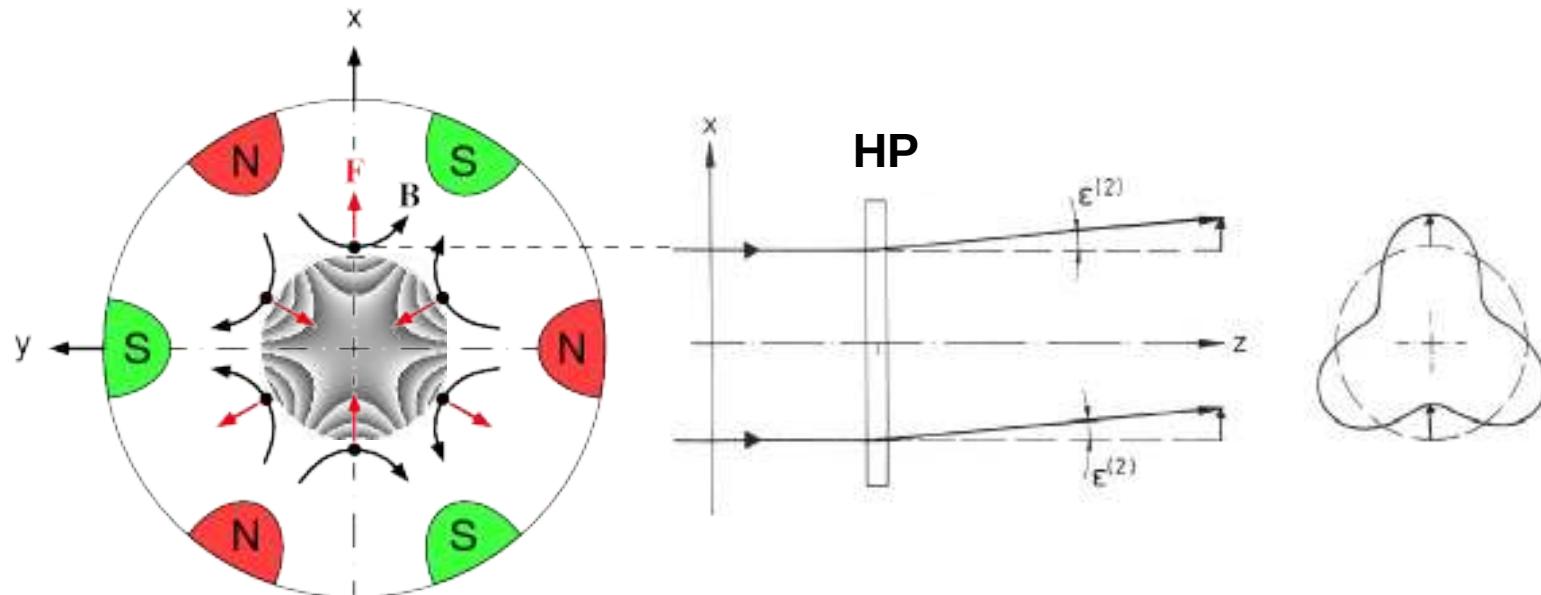


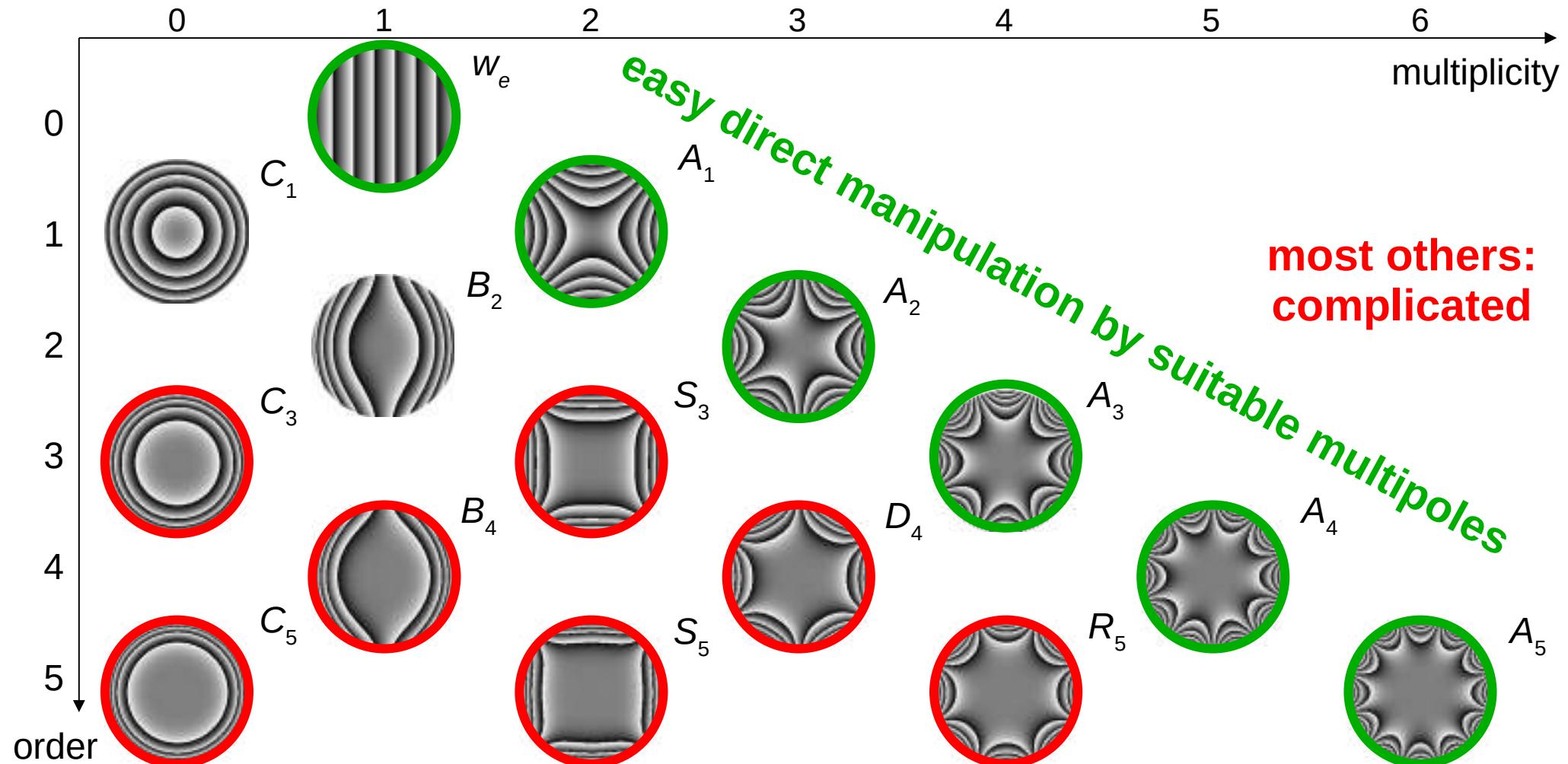
Quadrupoles – 2-fold Stigmators





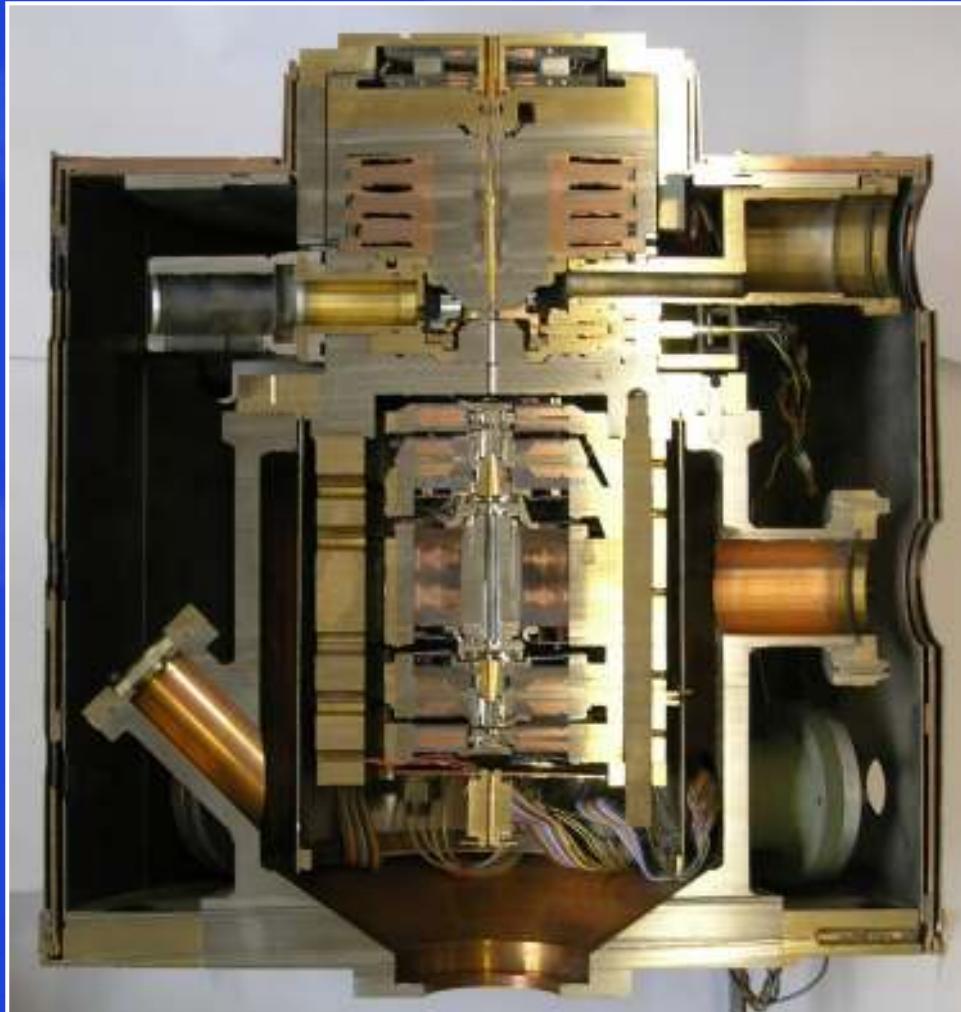
Hexapoles – 3-fold Stigmators



Wave aberration χ 



Long history of aberration correction



Darmstadt 1980 C_c - C_s -corrector Scherzer & Rose

Aberration correction was successfully shown in principle but did not improve the image resolution of the electron microscope.

- lack of precision machining
- lack of stability
- lack of aberration measurement
- ...

→ **No more funding ...**

same outcome world-wide
e.g. in Chicago and Cambridge

Aberration correction using hexapoles



Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

H. Rose

Institut für Angewandte Physik Technische Hochschule Darmstadt, FRG

Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope. A spherically corrected semiaplanatic objective lens for a subangstrom medium-voltage transmission electron microscope (TEM) is outlined. The aplanatic corrector consists of two telescopic round-lens doublets and two sextupoles centered about the nodal points of the second doublet. If the corrector is incorporated into a 300 kV TEM equipped with a field emission gun a resolution limit of 0.6 Å and 10^4 equally-well-resolved image points per diameter can be obtained. For achieving this performance the magnetic field of the objective lens must be stabilized with a relative accuracy of 1 ppm, while the fields of the corrector elements require at most a stability of 10 ppm.

Entwurf eines sphärisch korrigierten semiaplanatischen Mittelspannungs-Elektronenmikroskops. Eine in dritter Ordnung sphärisch korrigierte rein magnetische Objektivlinse, deren isotrope Koma beseitigt ist, wird vorgeschlagen. Das korrigierte Objektiv besteht aus einer Objektivlinse, zwei teleskopischen Rundlinsen-Dubletts und zwei Sextupolen, deren Mitten in den Knotenebenen des zweiten Dubletts liegen. Falls der Korrektor in ein 300 kV Transmissions-Elektronenmikroskop eingebaut wird, das mit einer Feldemissionskathode ausgestattet ist, können 10^4 Bildpunkte pro Durchmesser mit einer Auflösungsgrenze von 0.6 Å gleich gut aufgelöst werden. Um eine solche Auflösung zu erzielen, müssen die Beschleunigungsspannung und das Magnetfeld der zu korrigierenden Objektivlinse auf 1 ppm stabil gehalten werden. Für die Felder der Korrektorelemente genügt dagegen eine Stabilität von 10 ppm.

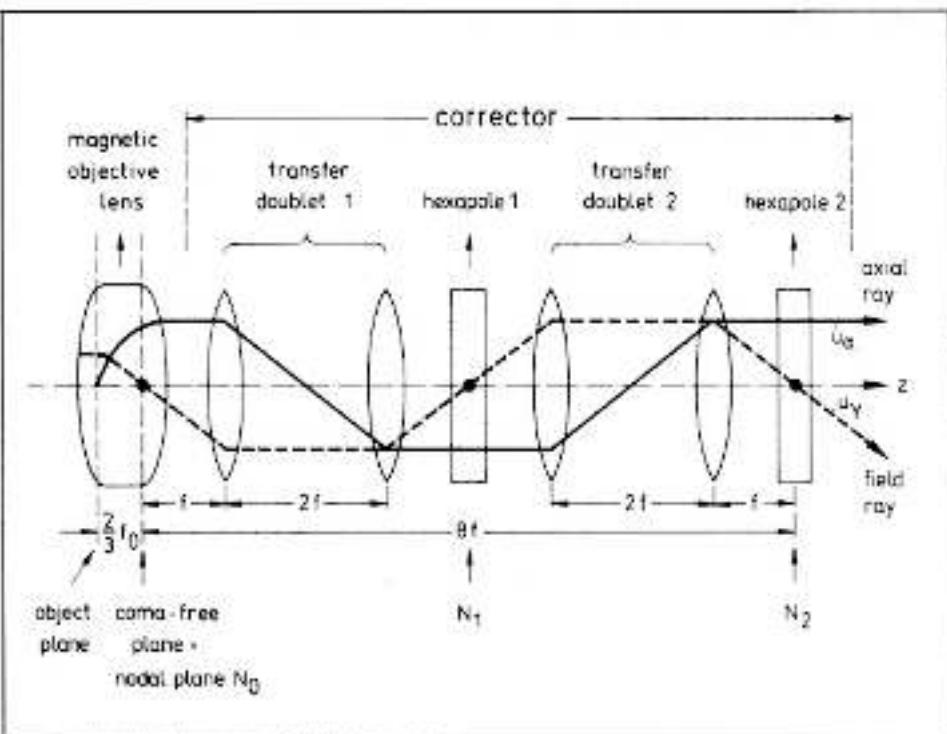


Fig. 2. Schematic arrangement of the elements of the spherically corrected semiaplanatic objective lens.



Aberration correction by means of hexapoles

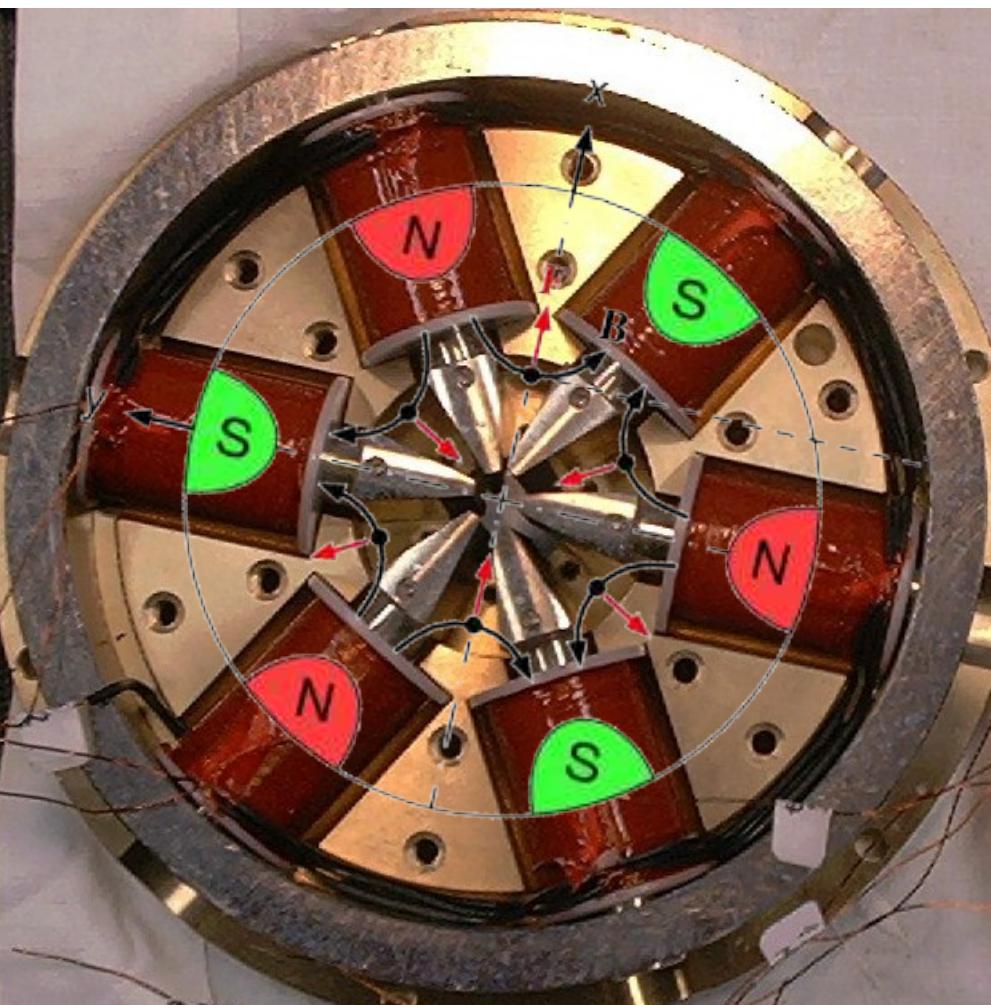
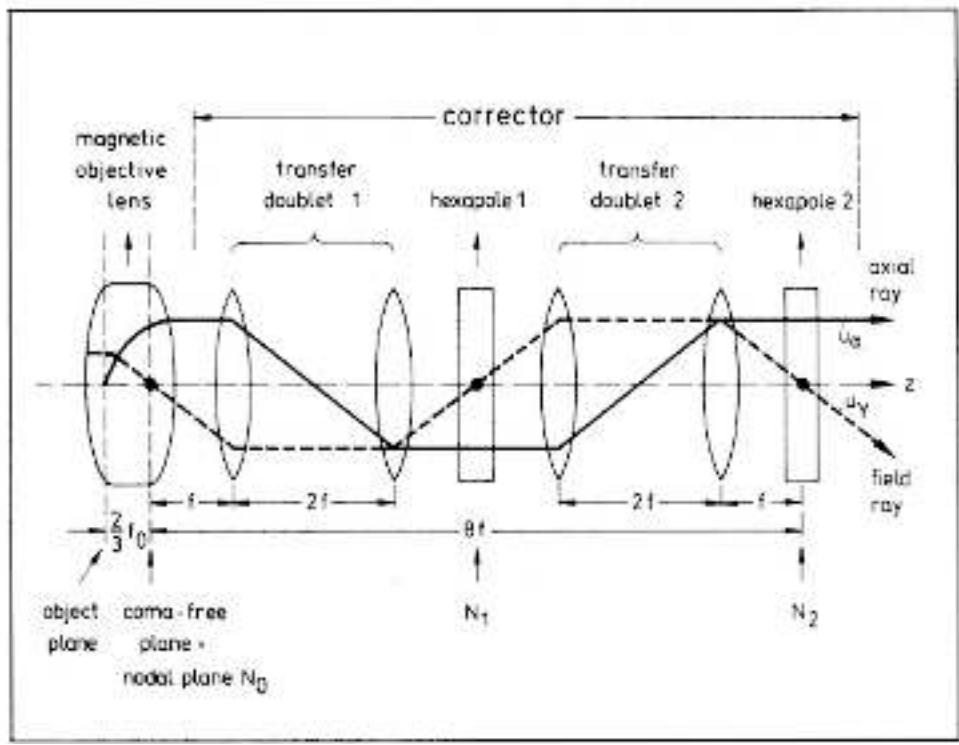
Opik

IS. No. 1 (1980) 15-34 © Wissenschaftliche Verlagsgesellschaft mbH, Stuttgart

Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

H. Rose

Institut für Angewandte Physik Technische Hochschule Darmstadt, FRG





Aberration correction by means of hexapoles

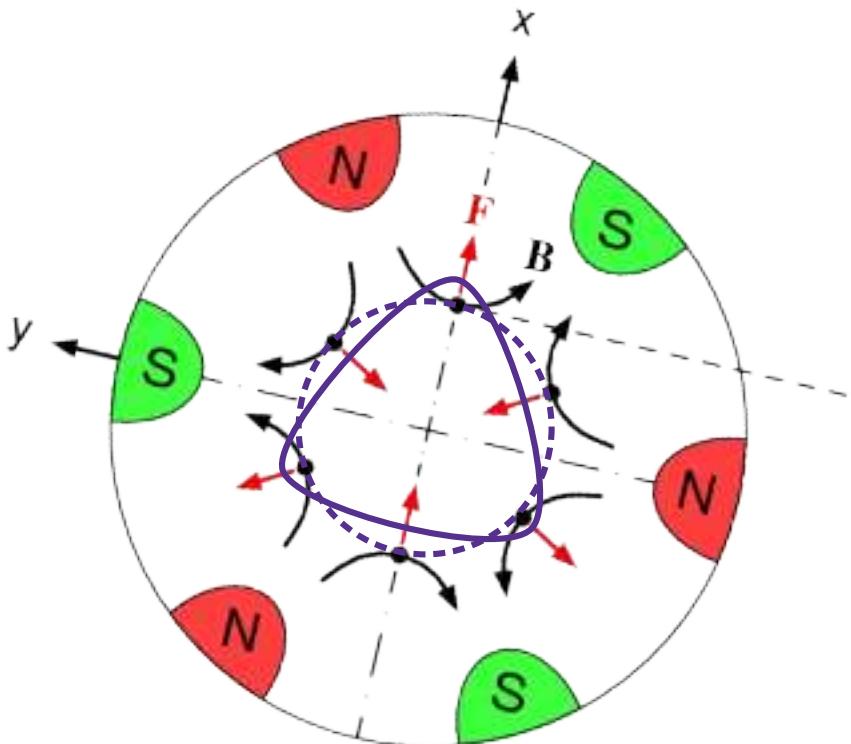
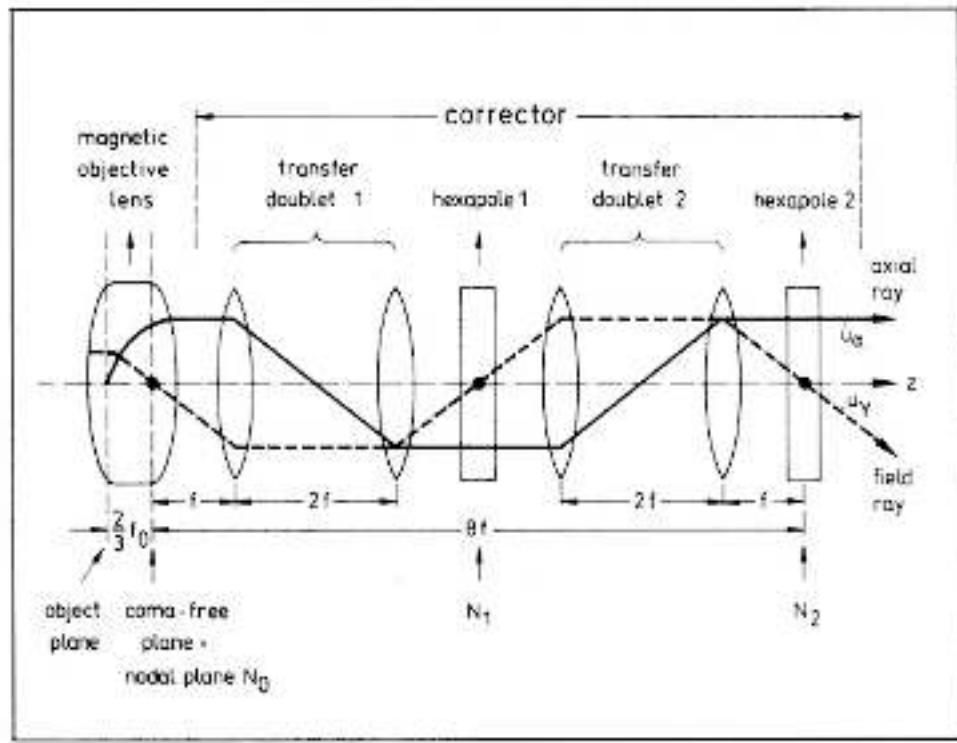
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Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

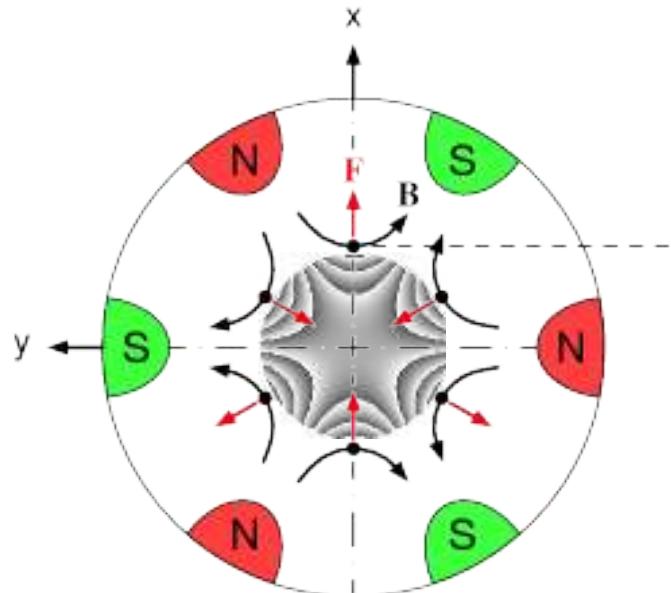
H. Rose

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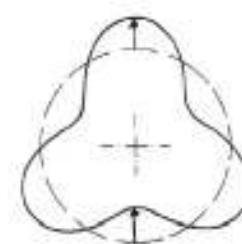
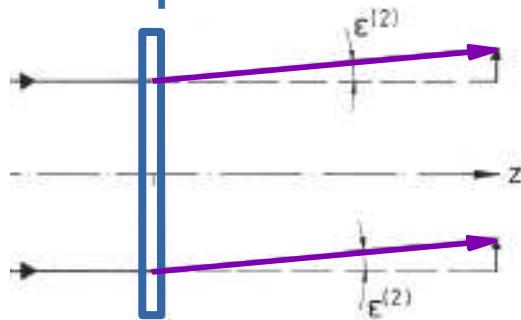




Aberration correction by means of hexapoles



short
hexapole

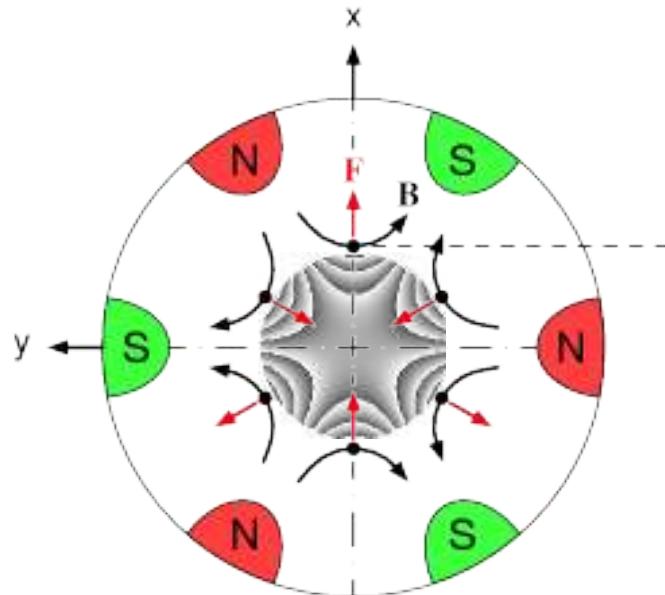


linear

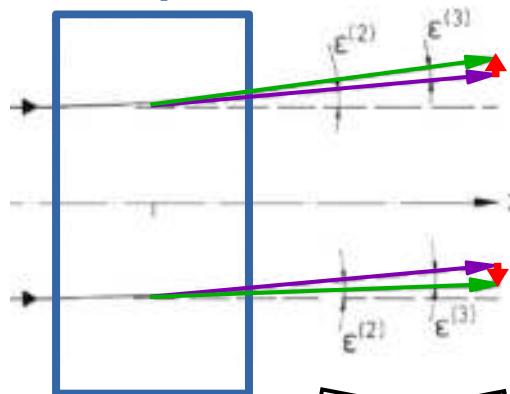
2nd order aberration
(three-fold astigmatism)



Aberration correction by means of hexapoles

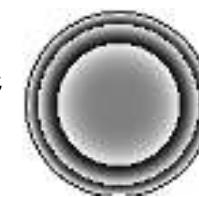
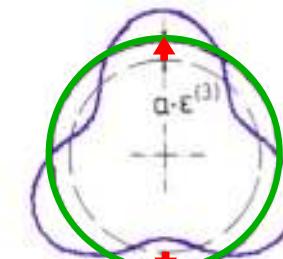


extended
hexapole



linear

quadratic



2nd order aberration
(three-fold astigmatism)

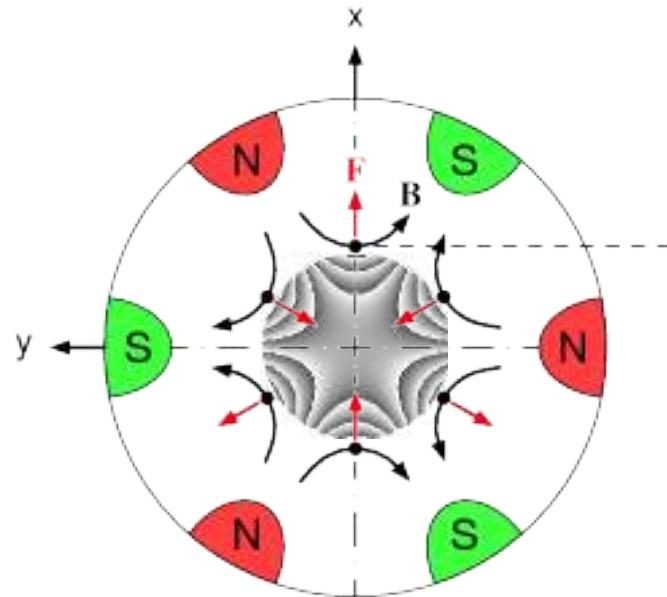
3rd order aberration
(negative spherical aberration)

Peter W. Hawkes: "The geometrical aberrations of general electron optical systems",
Philos. Trans. R. Soc. Lond. A, 257 (1965), 479-552.

Vernon D. Beck: "A hexapole spherical aberration corrector", Optik. 53 (1979), 241–255.

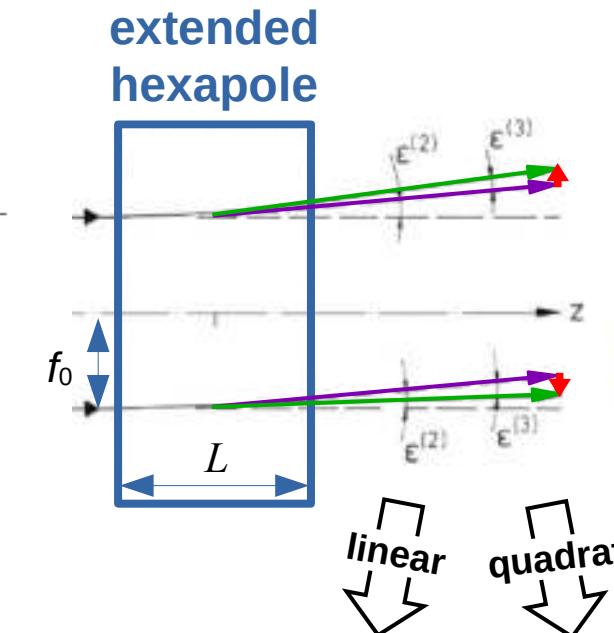


Aberration correction by means of hexapoles



Ψ_{3S} ... magnetic potential
 L ... hexapole length
 f_0 ... paraxial ray height

η ... constant: $\eta = \sqrt{\frac{|e|}{2m_0 U_0^*}}$



2nd order aberration
(three-fold astigmatism)

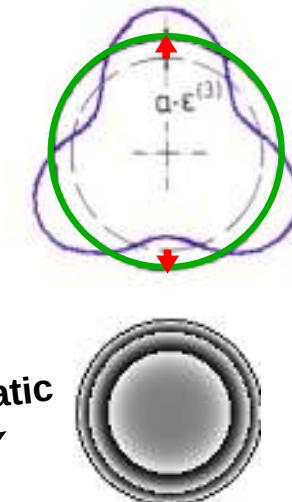
$$A_2 = 3 \eta \Psi_{3S} L f_0^3$$

linear

3rd order aberration
(negative spherical aberration)

$$C_3 = -3 |\eta \Psi_{3S}|^2 L^3 f_0^4 < 0$$

quadratic





Aberration correction by means of hexapoles

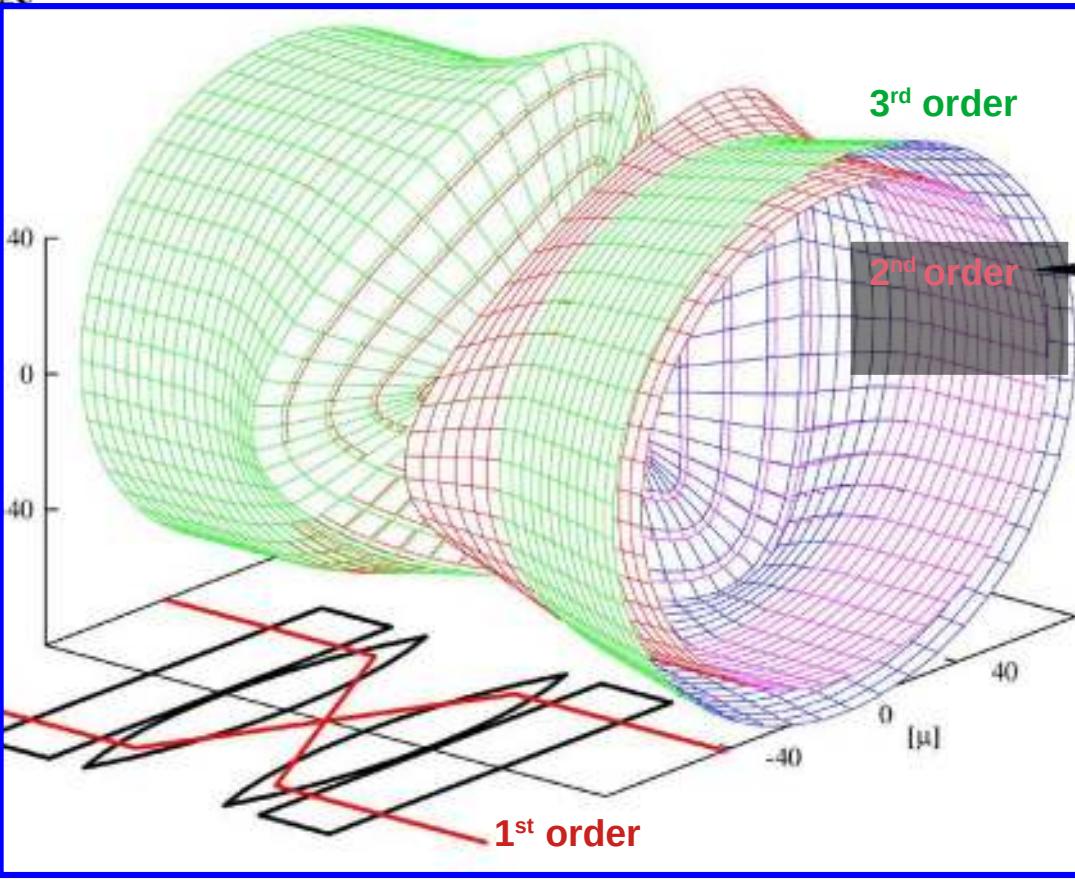
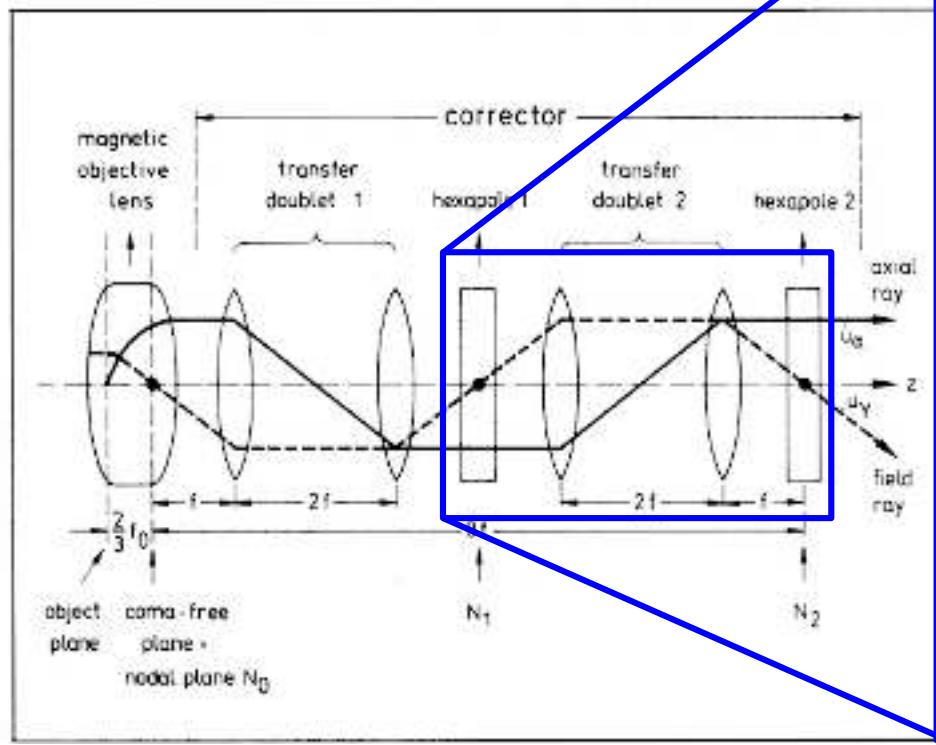
Opik

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Outline of a spherically corrected semiaplanatic medium-voltage transmission electron microscope

H. Rose

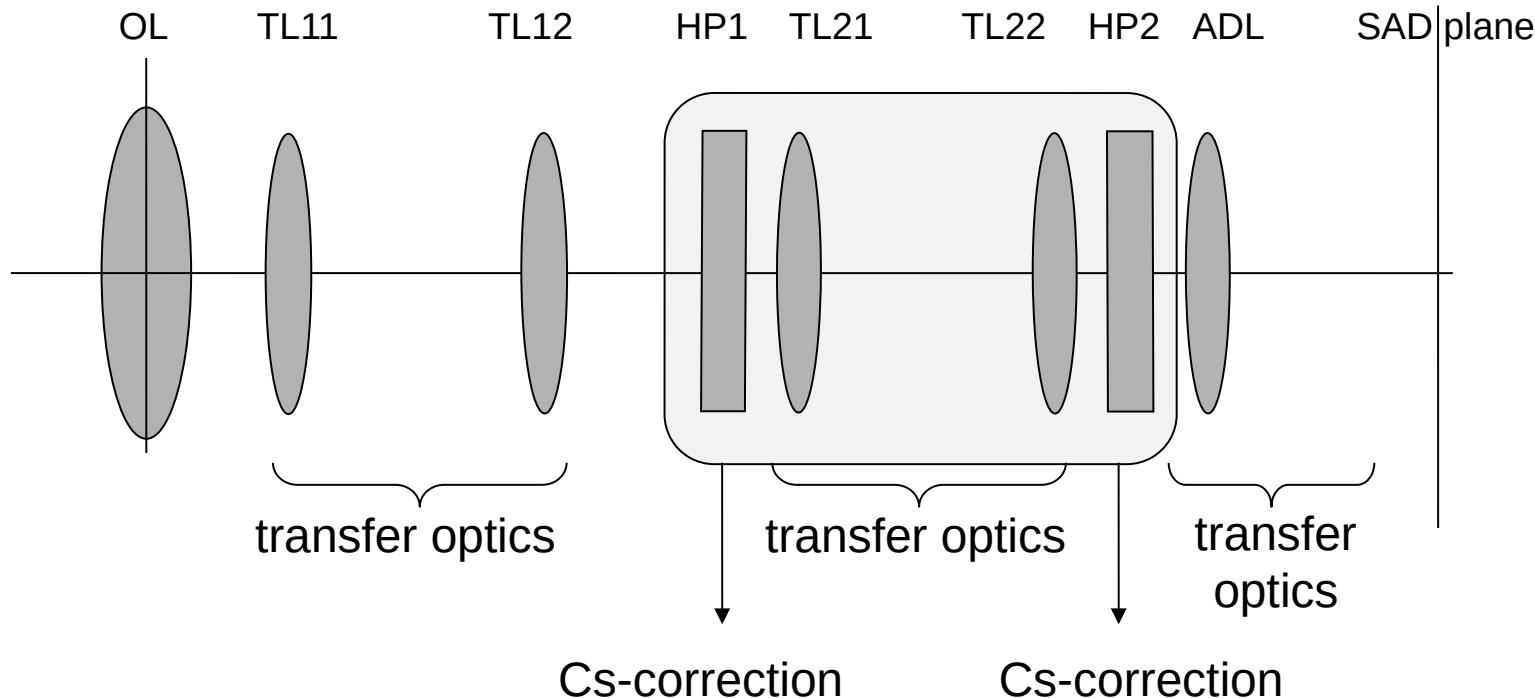
Institut für Angewandte Physik Technische Hochschule Darmstadt, FRG





Aberration correction by means of hexapoles

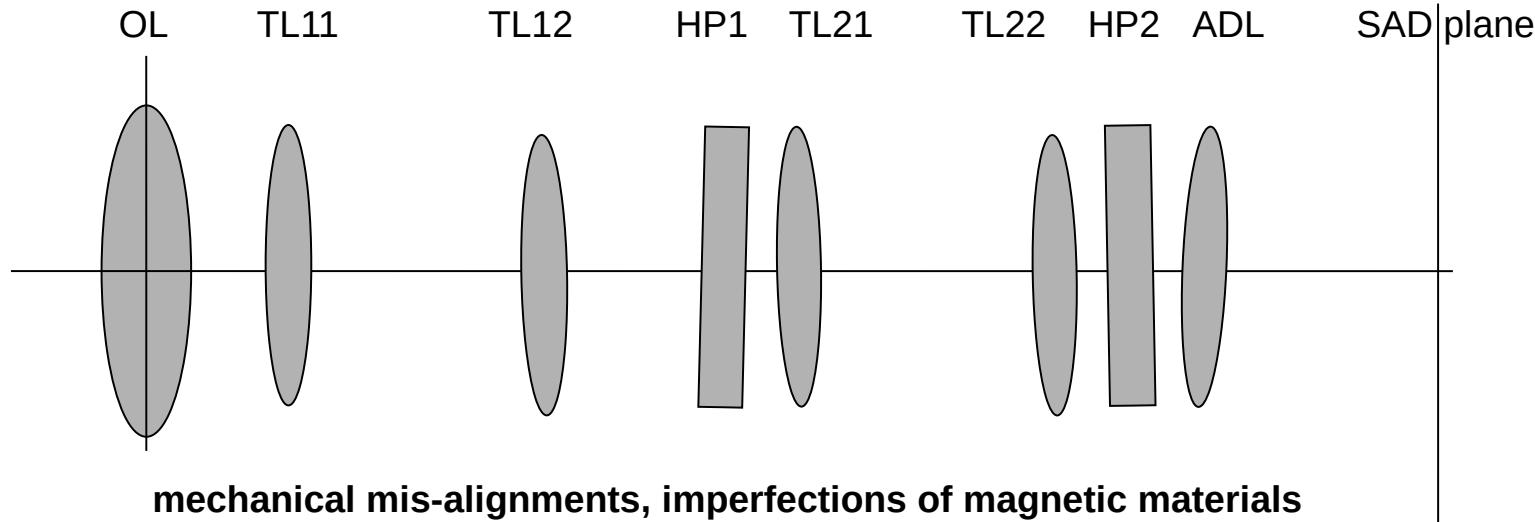
Ideal system:





Aberration correction by means of hexapoles

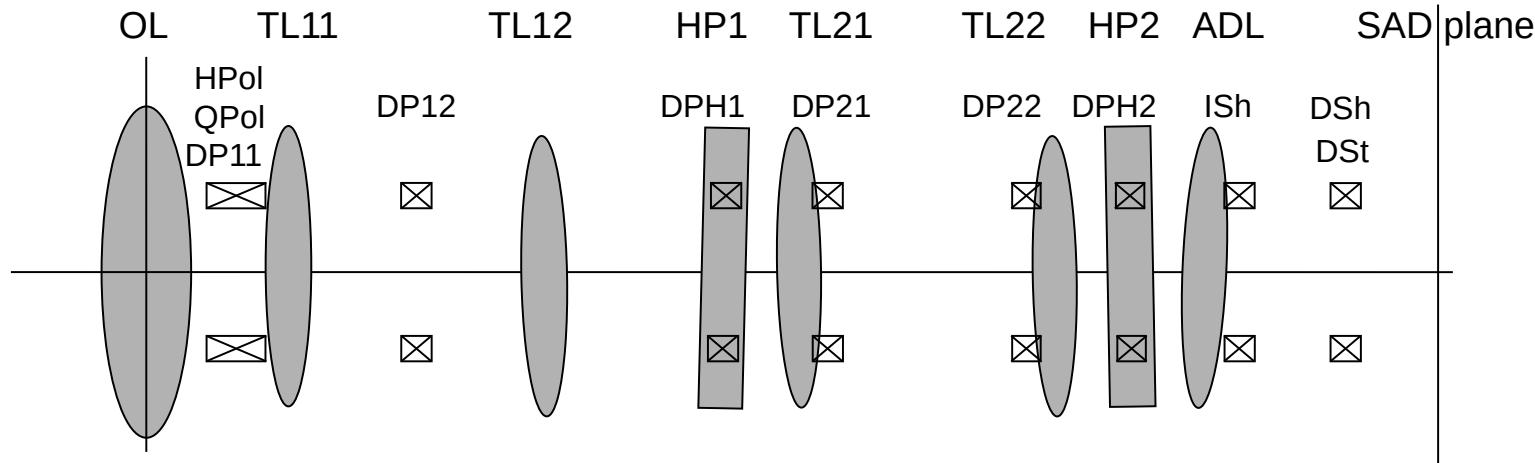
Ideal system vs. real system: small imperfections due to limited manufacturing precision





Aberration correction by means of hexapoles

Ideal system vs. real system: small imperfections due to limited manufacturing precision



mechanical mis-alignments, imperfections of magnetic materials

⇒ additional alignment channels required: deflectors, quadrupoles, hexapoles

Fundamental corrector alignment:

- Factory adjustment = fingerprint of machining tolerances and mechanical mis-alignments
- No change over time! ... *not even when moving a corrector to a different microscope*

Daily corrector alignment procedure:

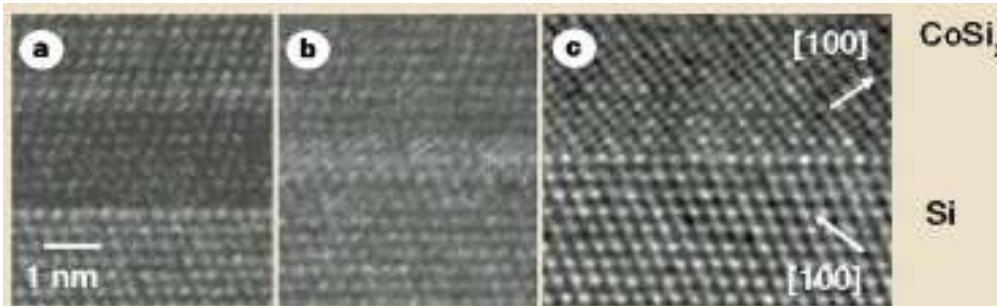
- Fine-tuning against hysteresis of magnetic elements and thermal drift.



1997: Breakthrough in C_s -correction for TEM



Prof. Max Haider



Electron microscopy
image enhanced

NATURE | VOL 392 | 23 APRIL 1998

Maximilian Haider*, Stephan Uhlemann*,
Eugen Schwan

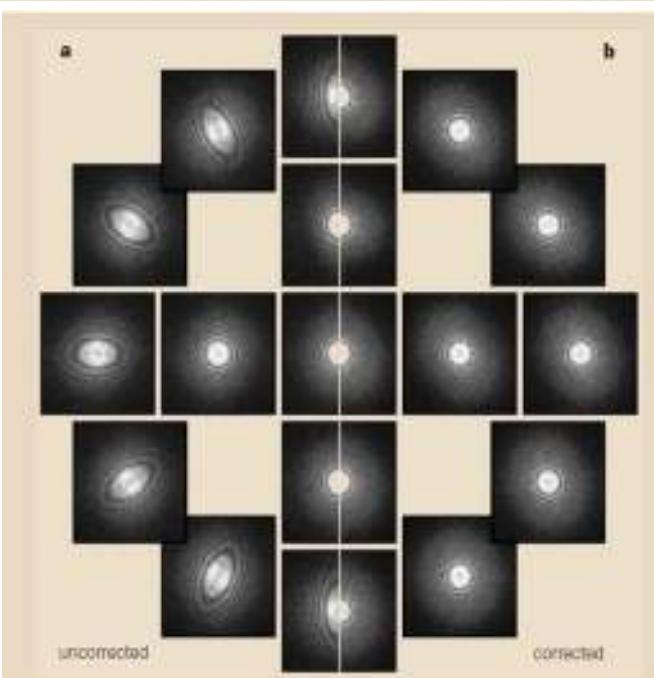
*European Molecular Biology Laboratory,
Postfach 102209, 69012 Heidelberg, Germany*

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Feld 519, 69120 Heidelberg, Germany

Harald Rose

*Institut für Angewandte Physik, Technische
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64289 Darmstadt, Germany*

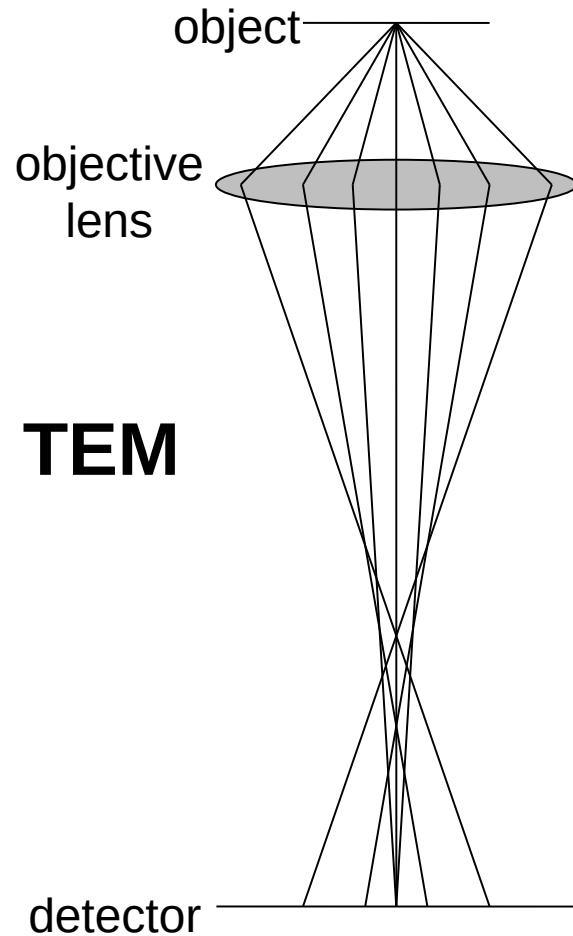
Bernd Käbius, Knut Urban
*Institut für Festkörperforschung,
Forschungszentrum Jülich GmbH,
52425 Jülich, Germany*



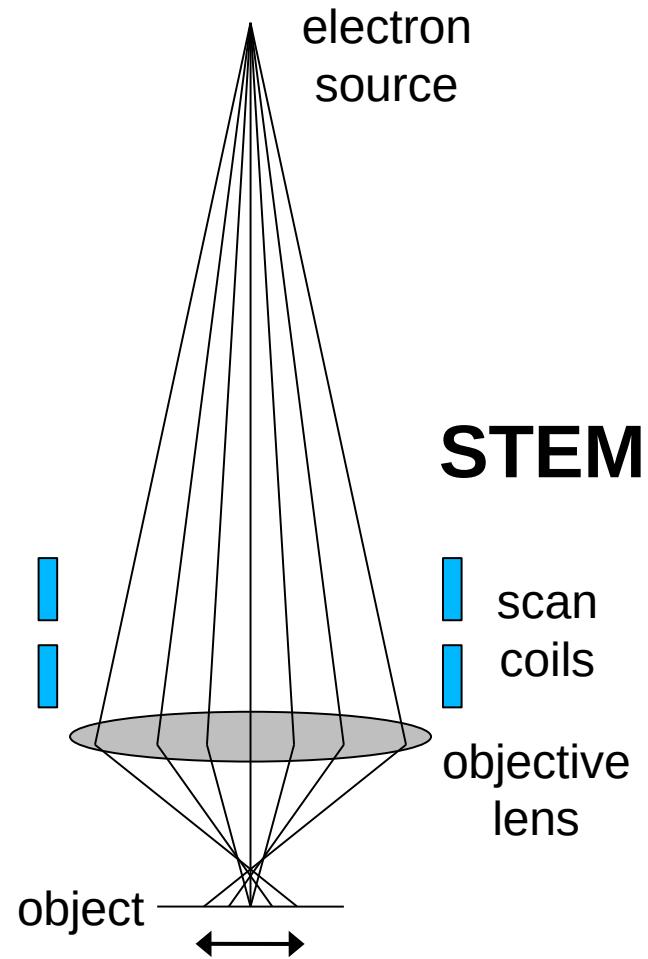
Philips CM200



Aberration-correction for TEM and STEM



TEM

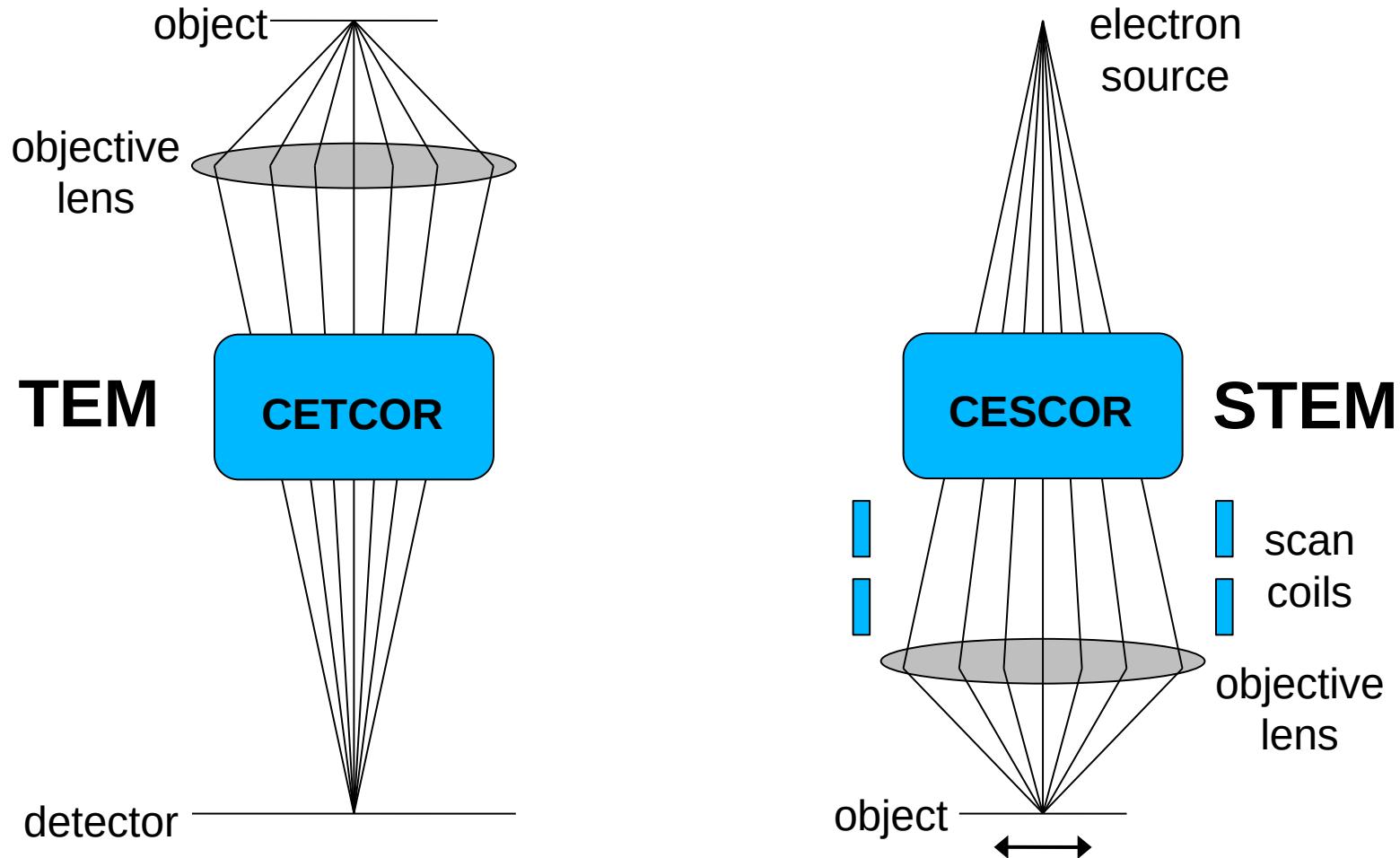


STEM

- scan coils
- objective lens

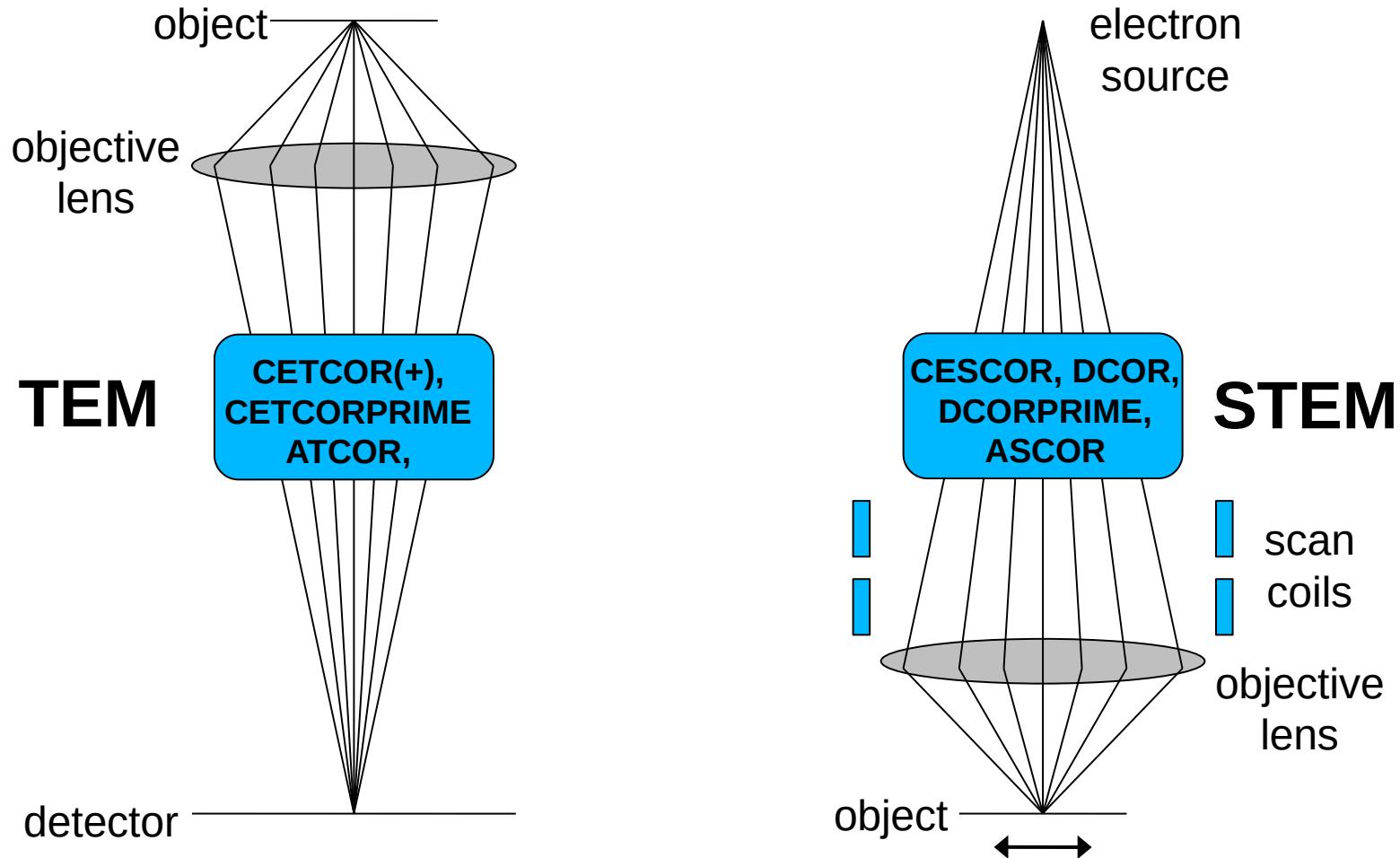


Aberration-correction for TEM and STEM



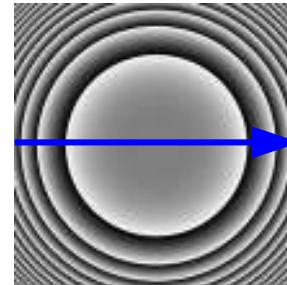
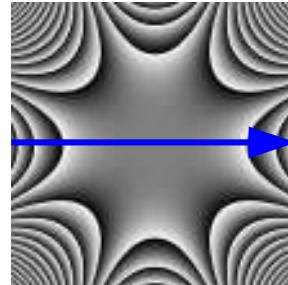


Aberration-correction for TEM and STEM



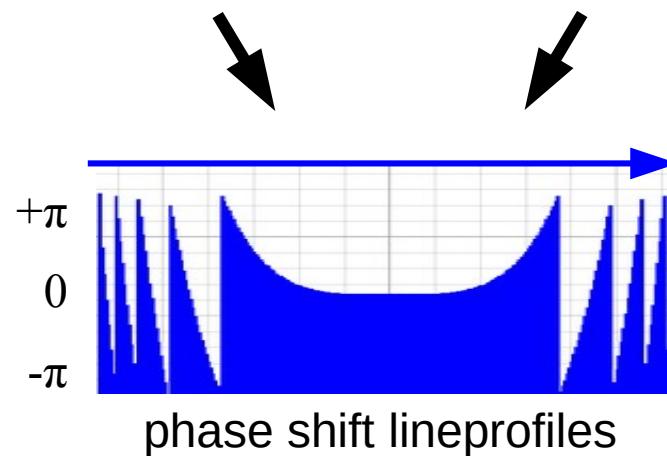
Aberration correction using quadrupoles and octupoles

C_s -correction by means of octupoles



phase shift in
octupole field

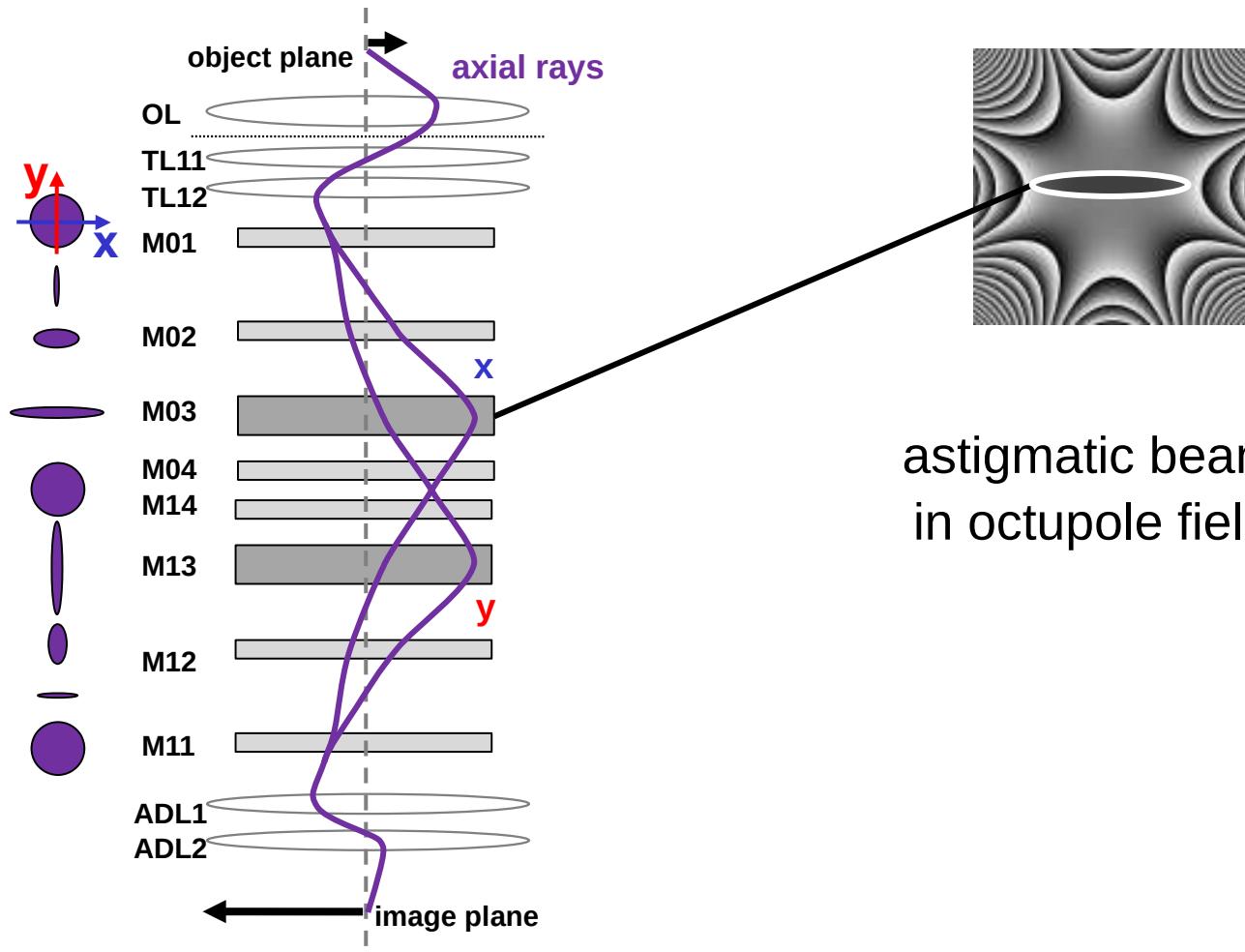
spherical
aberration



phase shift lineprofiles



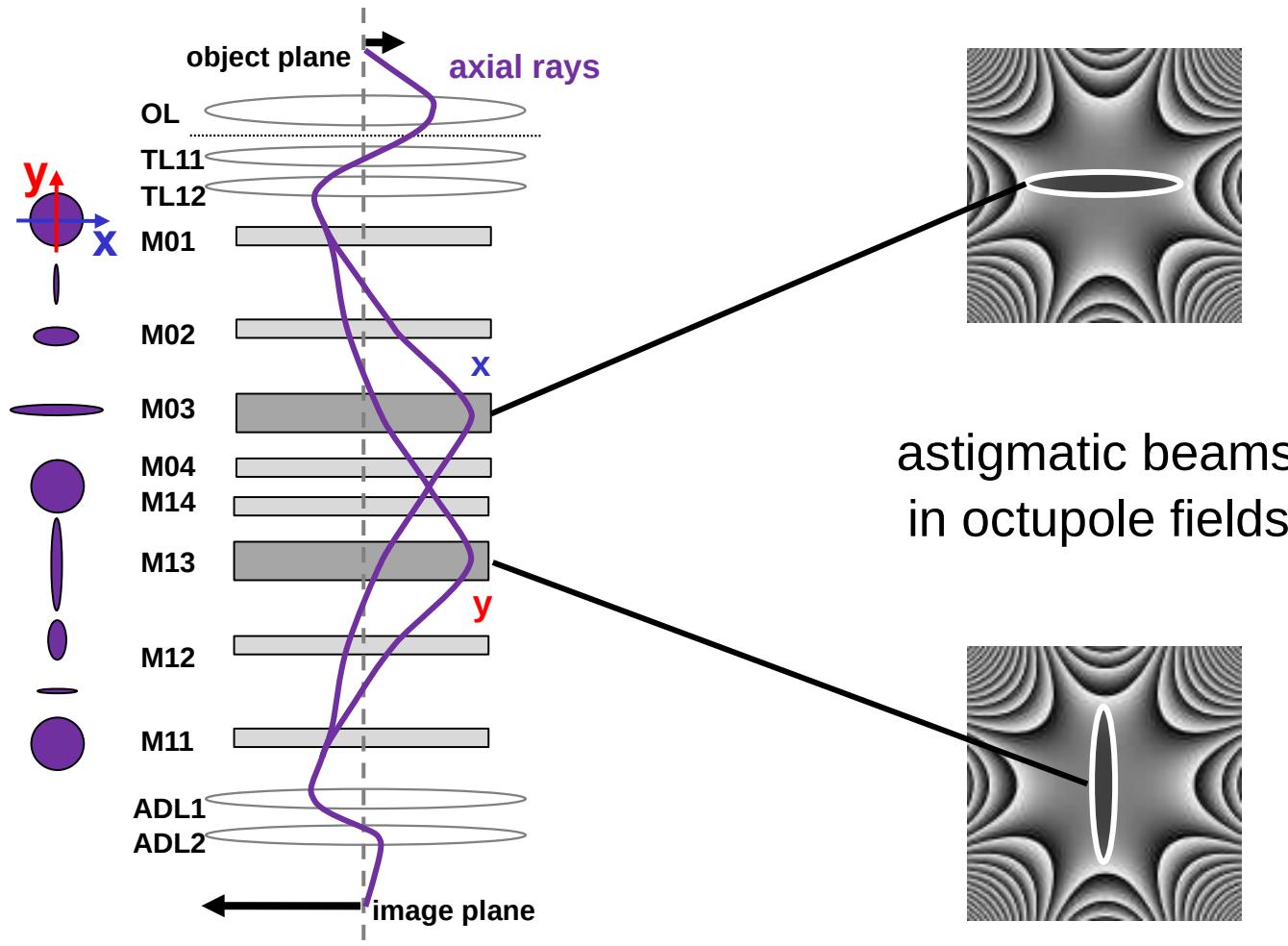
C_s -correction by means of octupoles



astigmatic beam
in octupole field



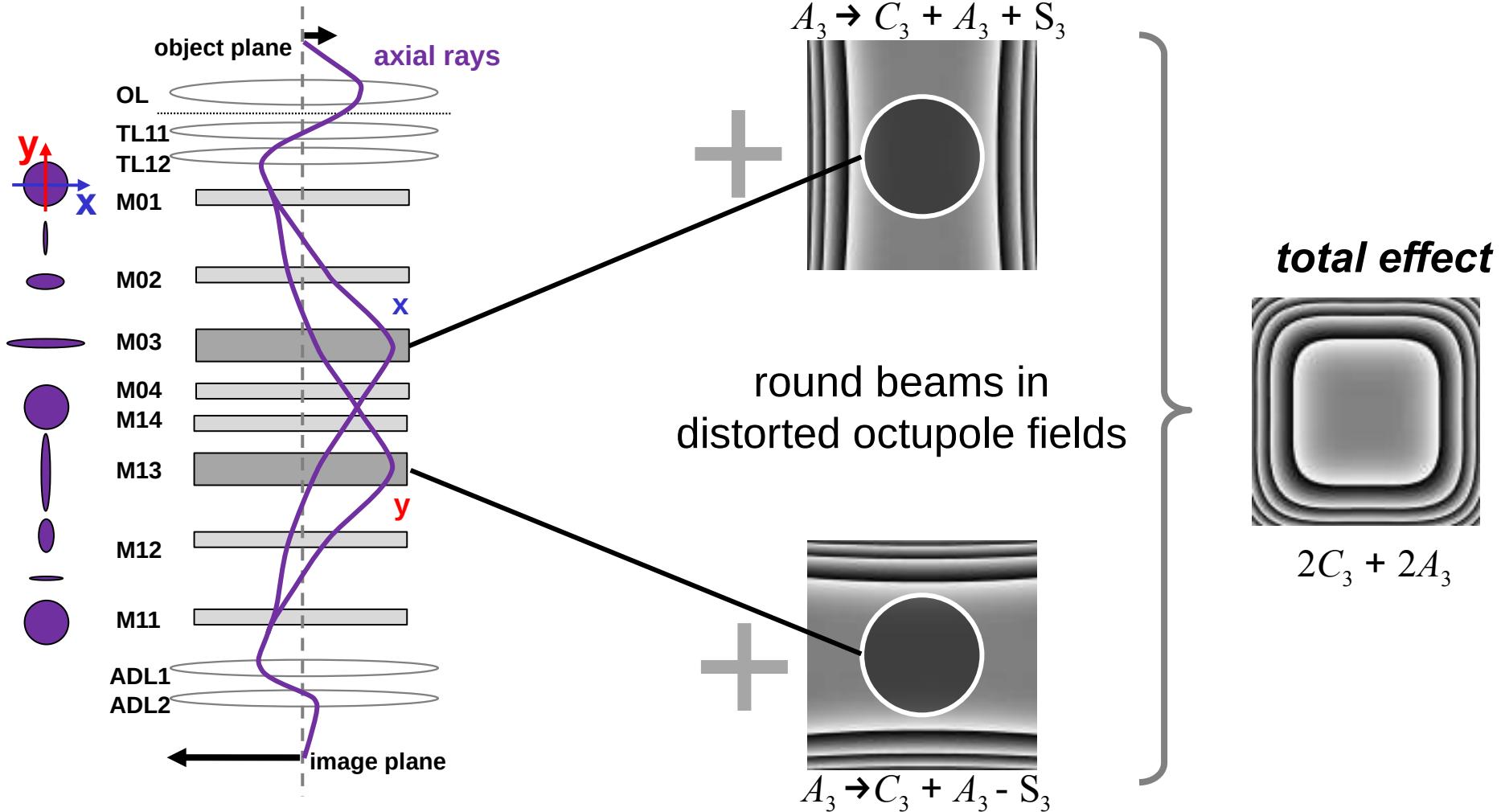
C_s -correction by means of octupoles



astigmatic beams
in octupole fields

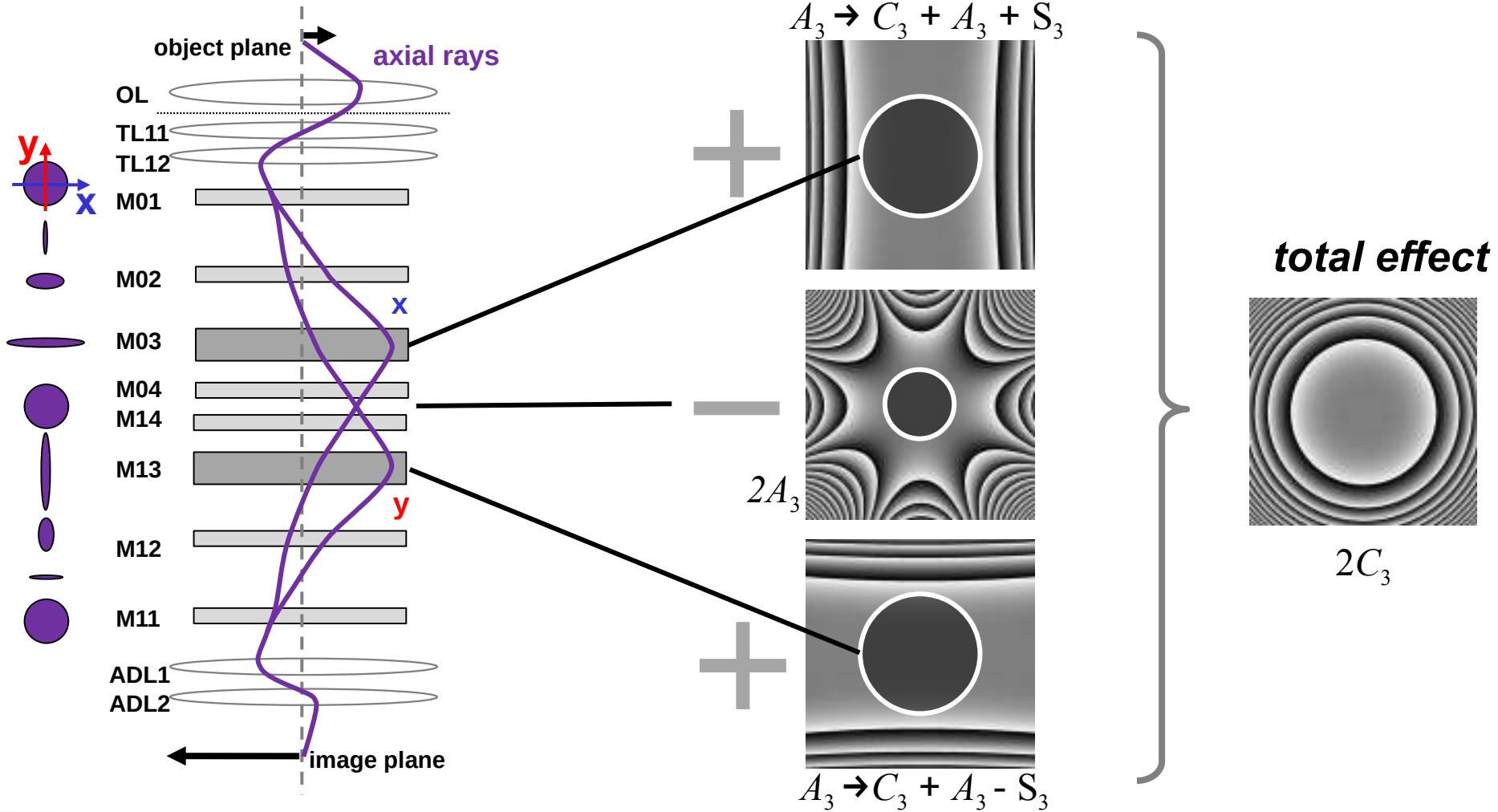


C_s -correction by means of octupoles





C_s -correction by means of octupoles

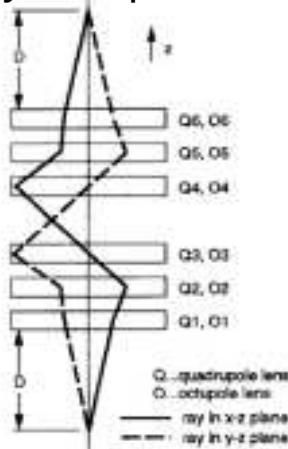




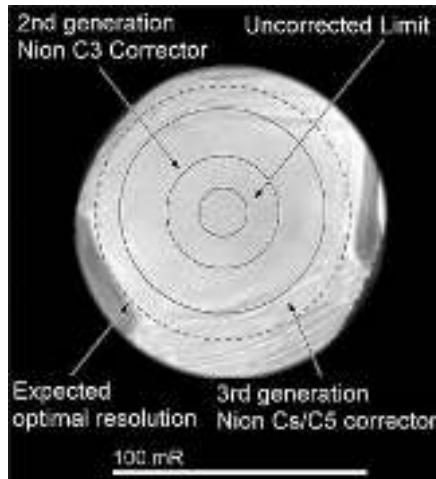
Niklas Dellby and ONdrey Krivanek



- Resolution improvement by Cs-correction in a VG HB5 STEM (1997) based on a 1964 concept from J. Deltrap, Cavendish labs (UK)
- Today: complete nion STEM column with monochromator and spectrometer



from: Krivanek et al. Inst. Phys.
Conf.Ser.153 (Proc. 1997 EMAG)



<http://www.nion.com>

Nion UltraSTEM 100

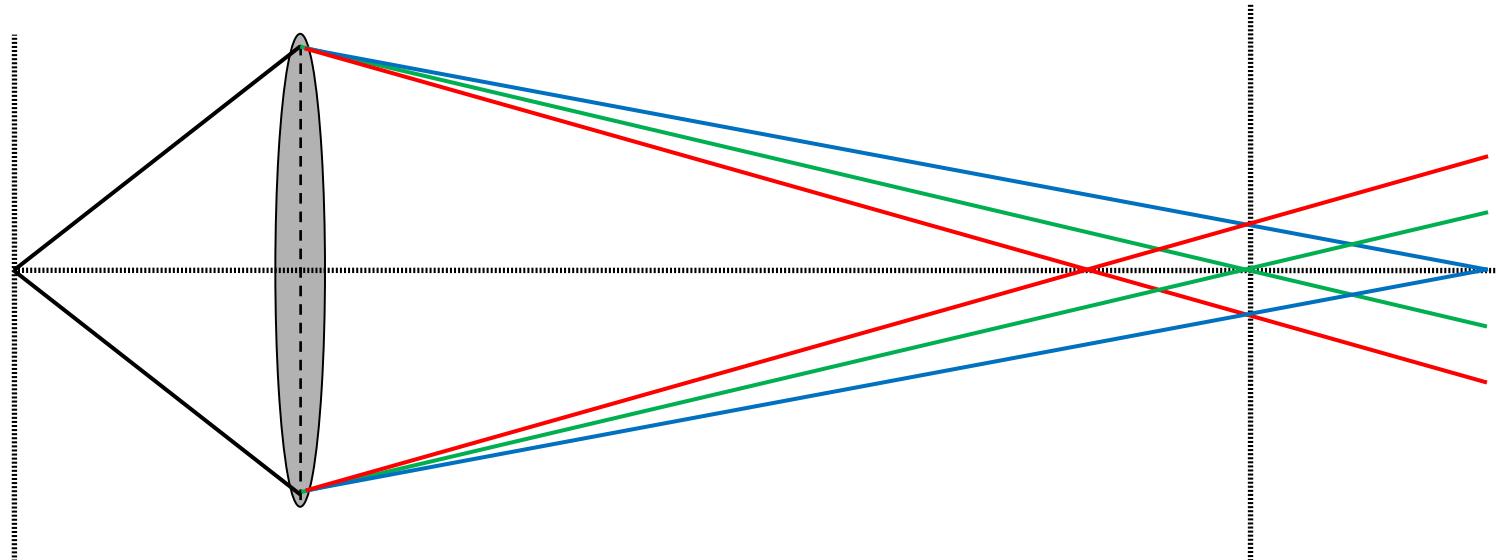


<http://www.nion.com>



Chromatic aberration

Electron energy: $E_0 - \Delta E < E_0 < E_0 + \Delta E$



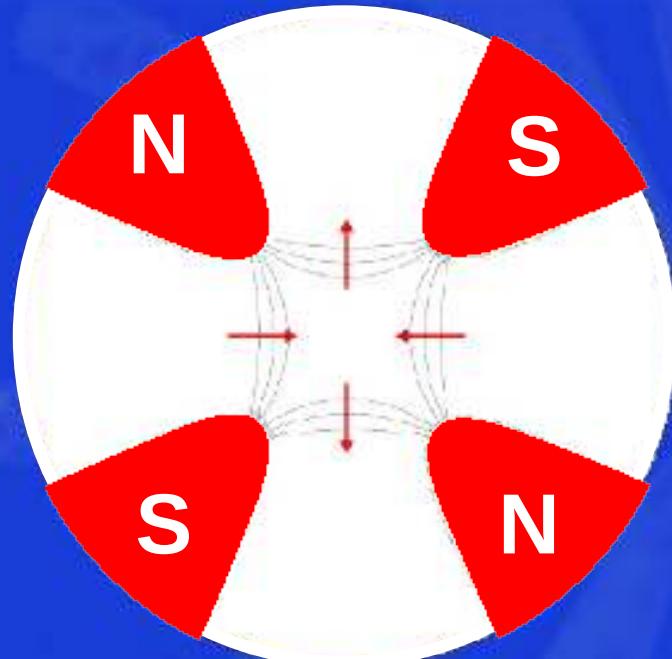
Object
plane

Gaussian
image plane

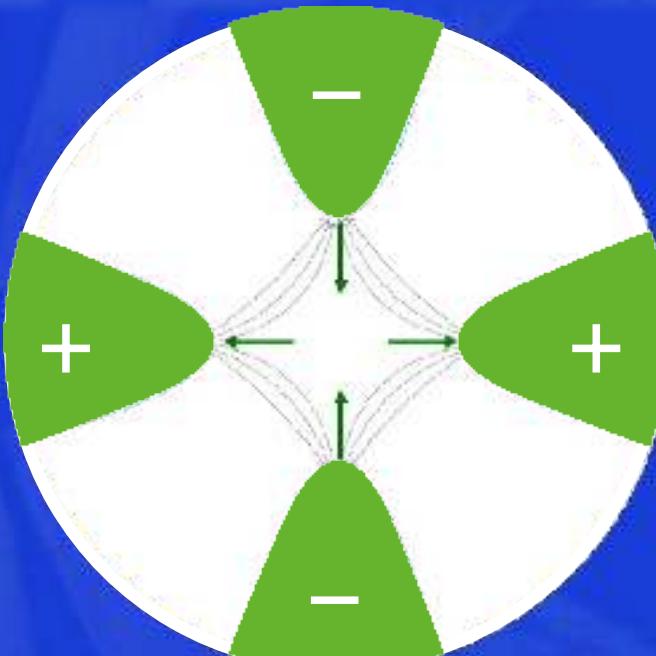


Chromatic aberration correction

magnetic QP



electric QP



$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$





Chromatic aberration correction

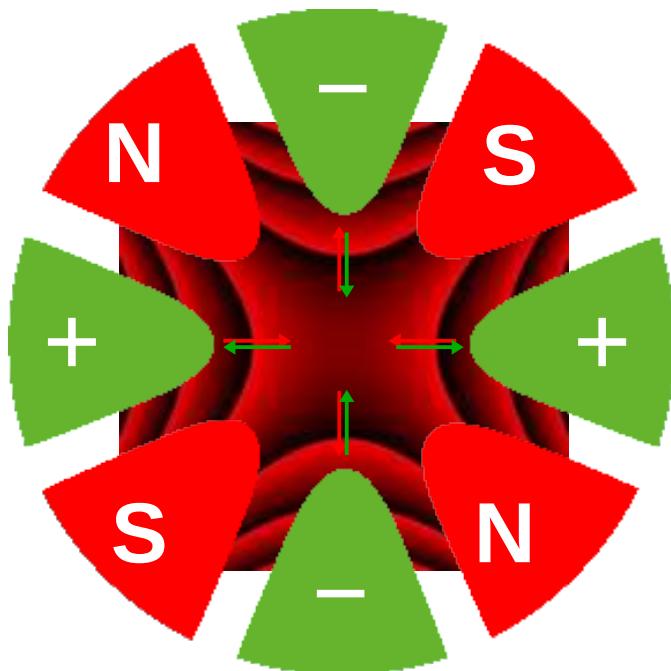
Crossed electric and magnetic fields:

equation of motion

$$\frac{d}{dt}(\vec{mv}) = -e(\vec{E} + \vec{v} \times \vec{B})$$



Wien filter: $= 0$
for exact energy E_0



$E < E_0$: quadrupole effect

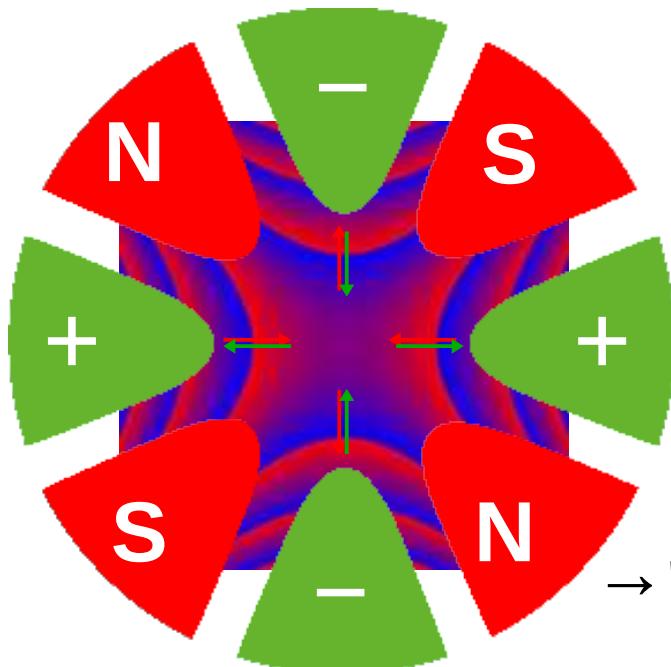


Chromatic aberration correction

Crossed electric and magnetic fields:

equation of motion

$$\frac{d}{dt}(\vec{m}\vec{v}) = -e(\vec{E} + \vec{v} \times \vec{B})$$



Wien filter: $= 0$
for exact energy E_0

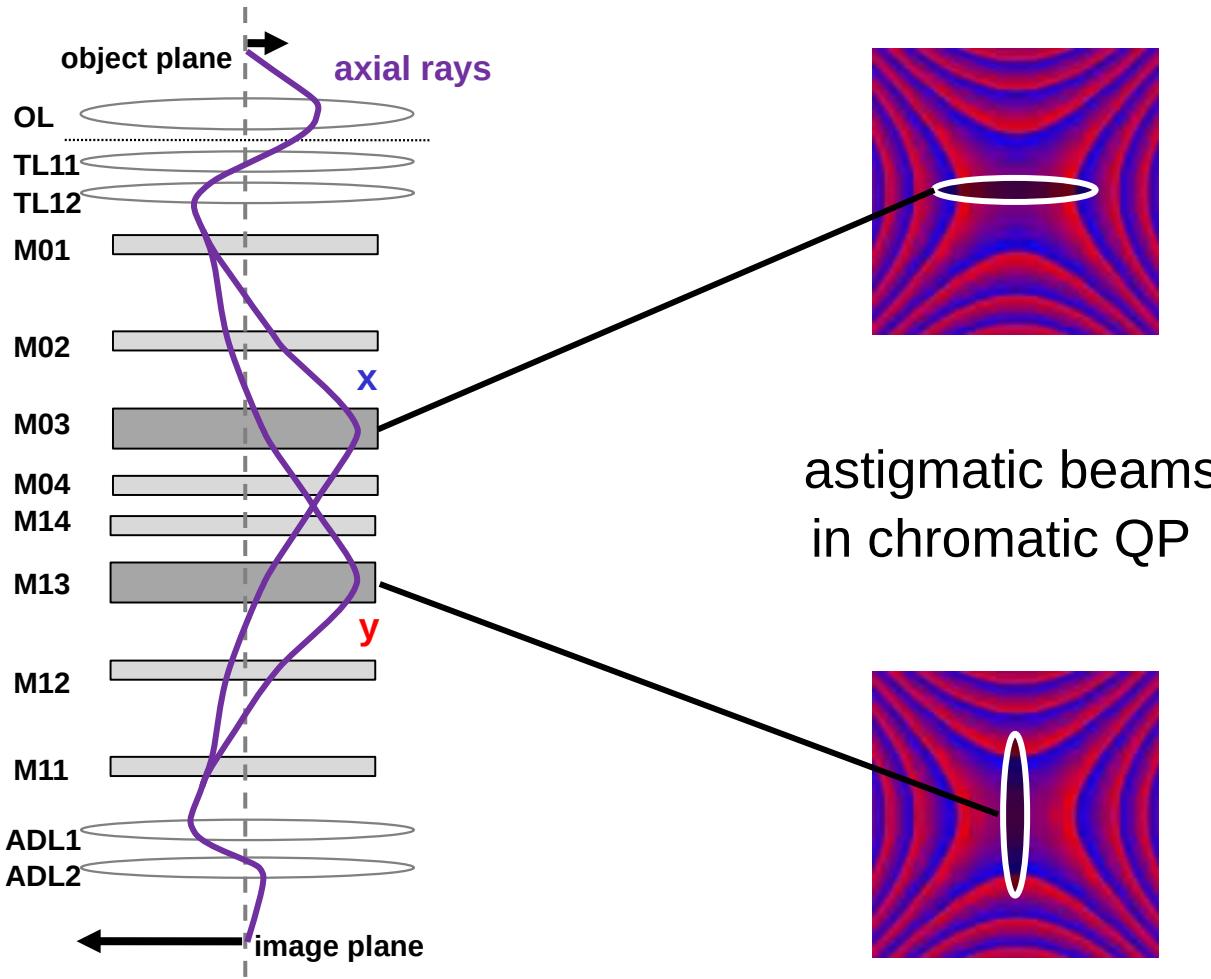
$E < E_0$: quadrupole effect

$E > E_0$: opposite QP effect

→ "chromatic quadrupole" A_{1c}

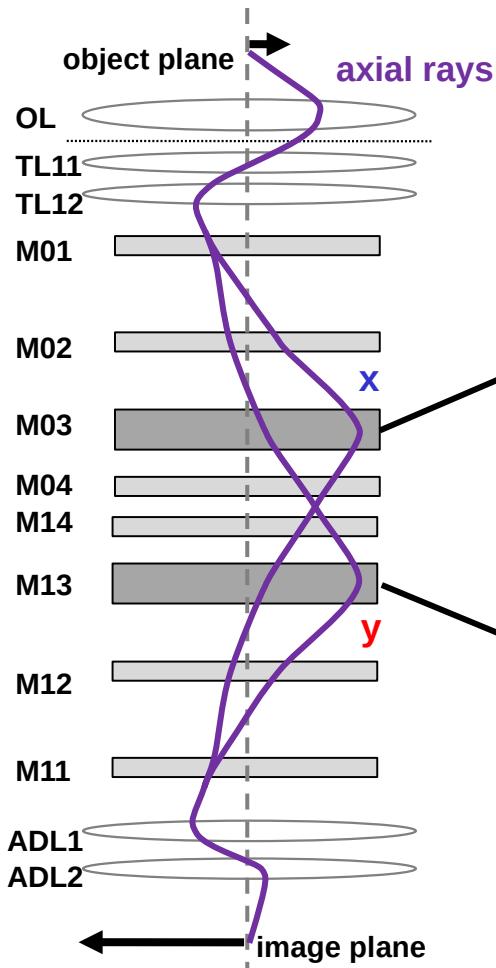


Chromatic aberration correction

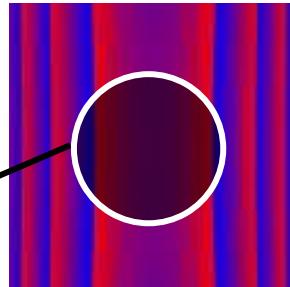




Chromatic aberration correction



$$A_{1c} \rightarrow A_{1c} + C_{1c}$$

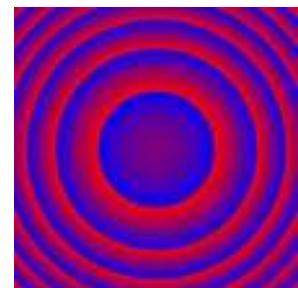


round beams in
distorted chromatic QP



$$A_{1c} \rightarrow A_{1c} - C_{1c}$$

total effect



$$-2C_{1c}$$



1995: First ever working and resolution improving corrector

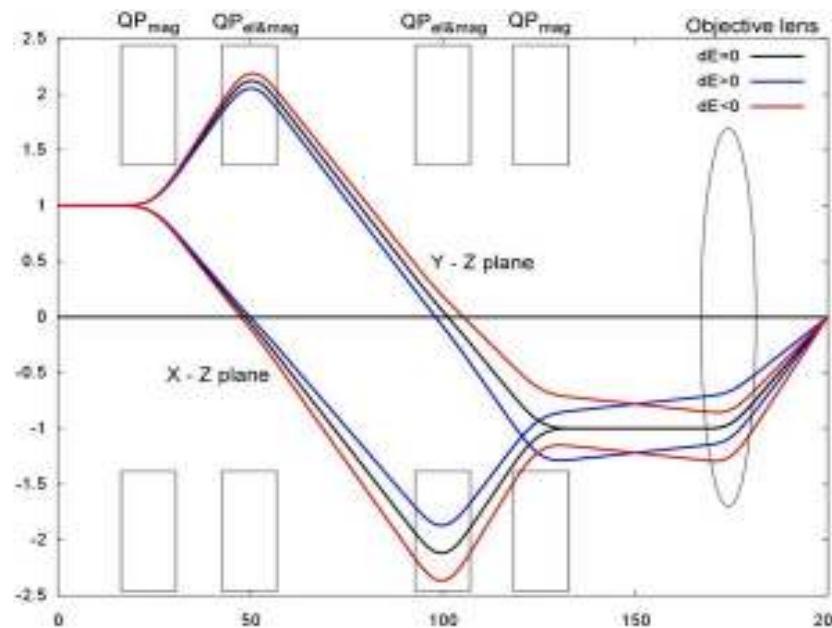
Optik

98, No. 3 (1995) 112–118

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Correction of spherical and chromatic aberration in a low voltage SEM

J. Zach, M. Haider





1995: First ever working and resolution improving corrector

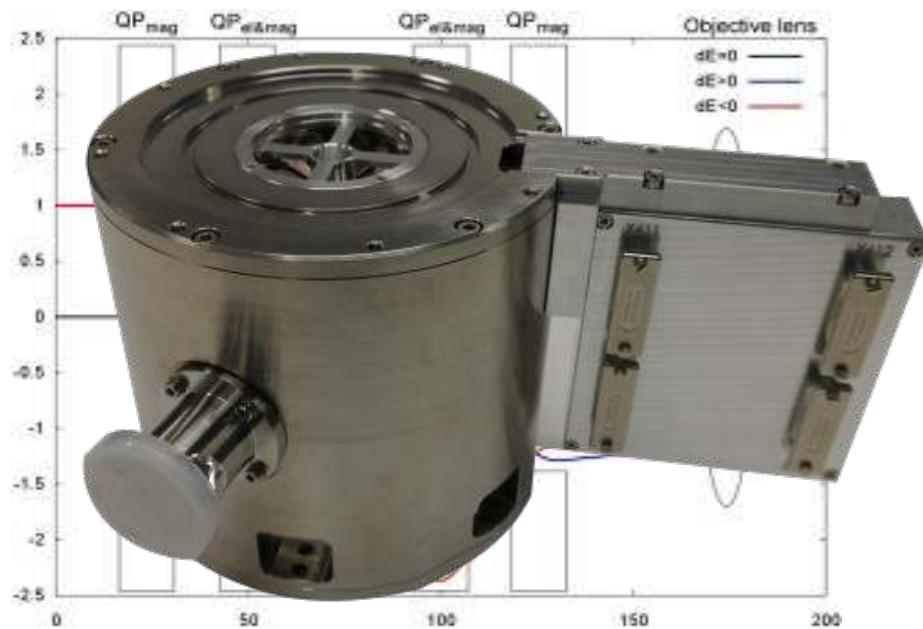
Optik

98, No. 3 (1995) 112–118

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Correction of spherical and chromatic aberration in a low voltage SEM

J. Zach, M. Haider



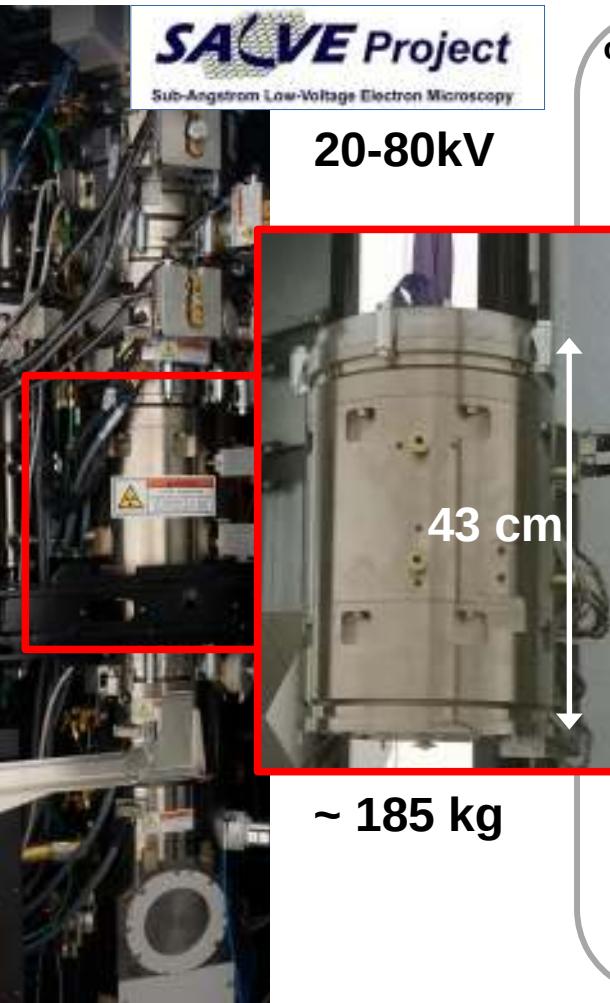


C_c - and C_s -correction for TEM

CCOR 30-300kV 160 channels

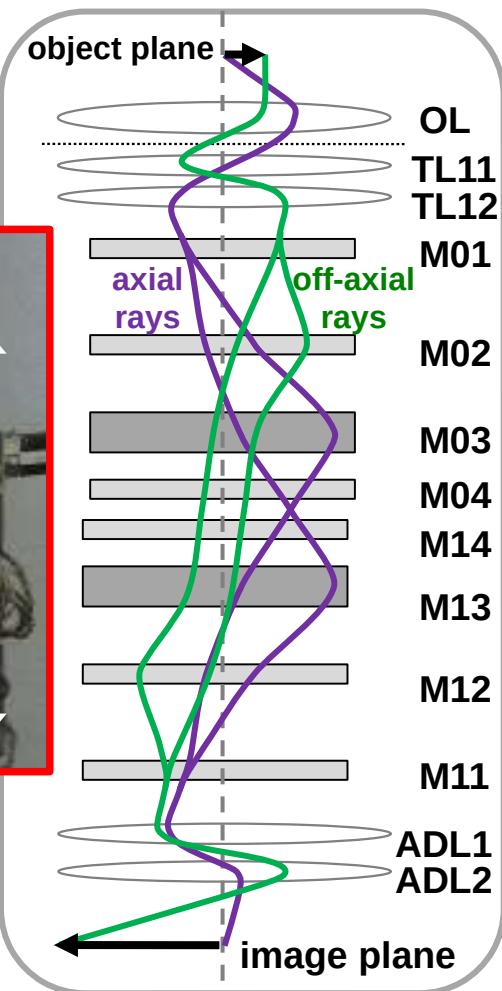


828 mm



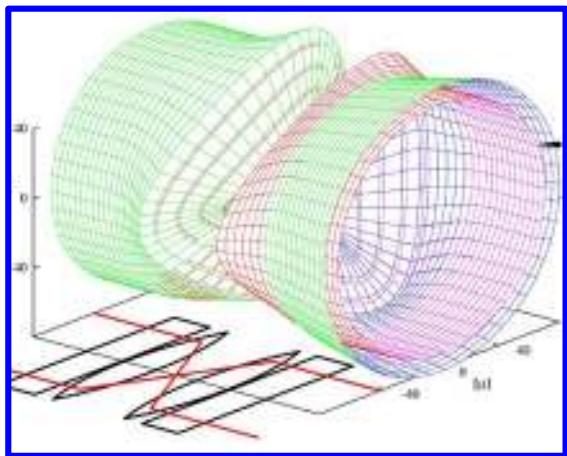
SALVE Project
Sub-Angstrom Low-Voltage Electron Microscopy

20-80kV

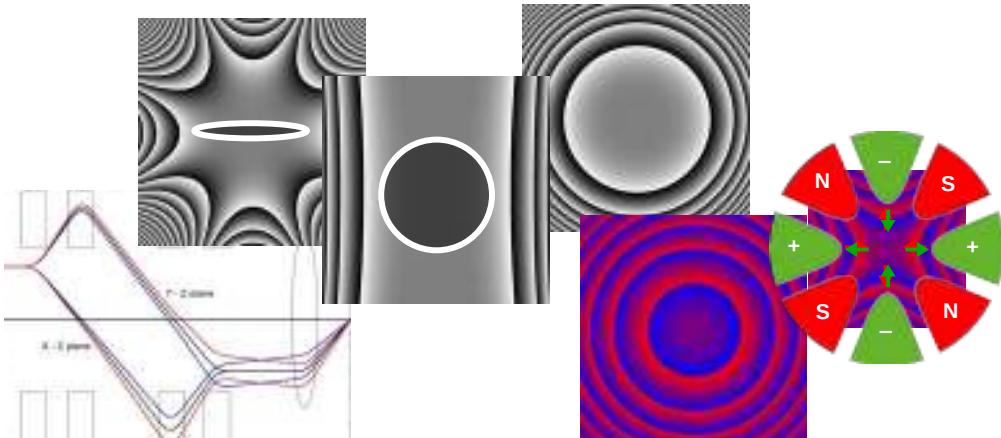




C_s -correction with hexapoles



C_C - C_S -correction with quadrupoles and octupoles



Further resources

R. Erni: "Aberration-Corrected Imagingin TEM" (second edition 2015).

P.W. Hawkes: "The correction of electron lens aberrations", Ultramicroscopy 156 (2015), A1-A64.

M. Haider et al.: "Present and Future Hexapole Aberration Correctors for High-Resolution Electron Microscopy", Advances in Imaging and Electron Physics, Volume 153, 43-119, ISSN 1076-5670.

H. Müller et al.: "Aberration-corrected optics: from an idea to a device", Physics Physics Procedia 1 (2008), 167–178.